

## UNIT NO 10

### -: SIMPLE HARMONIC MOTION AND WAVES :-

Oscillatory Motion: "The repeated back and forth motion about Certain Equilibrium (mean, Rest) position is Called Oscillatory Motion.

(OR)

" The to and fro motion of an object from its mean position (equilibrium position) is Called Oscillatory Motion.

Equilibrium position: " Position where an object tends to Comes at Rest When no external force is applied.

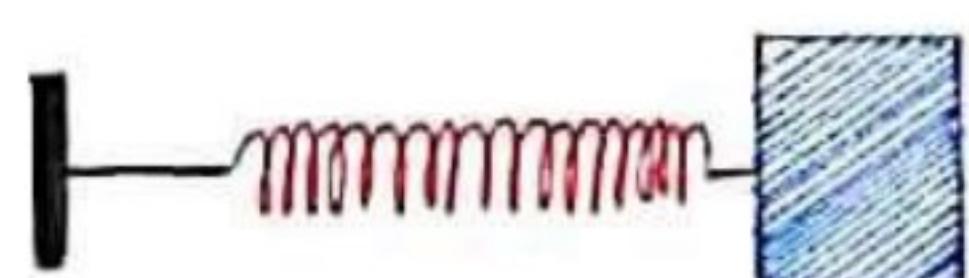
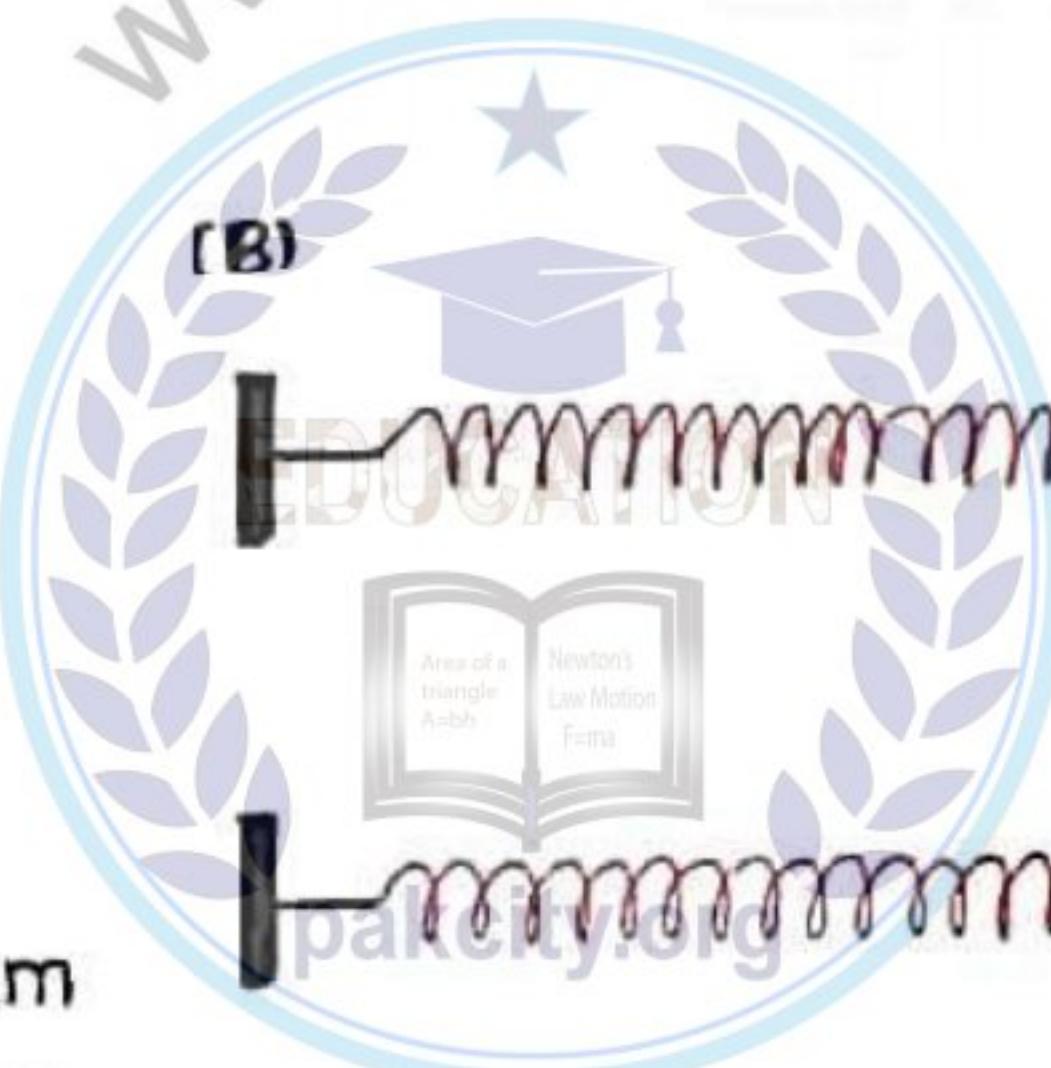
(OR)

" A State of a body where neither the internal energy nor the motion of the body changes With respect to time is Called Equilibrium position.

(A)



(Simple pendulum)



(Mass-Spring-System)

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EDUCATION

Area of a triangle  
A=  $\frac{1}{2}ab$   
Newton's Law Motion  
Fma

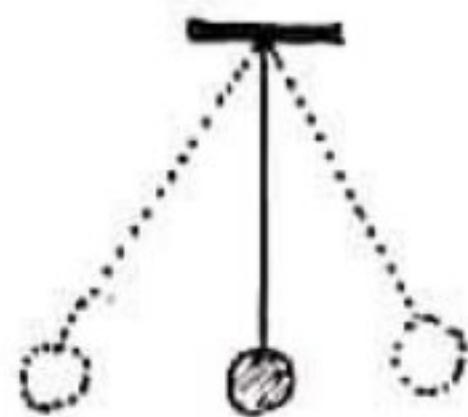
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(Equilibrium position)

## Examples Of oscillatory Motion:

The following are the examples of oscillatory Motion.

- (1) Motion of a Simple pendulum.

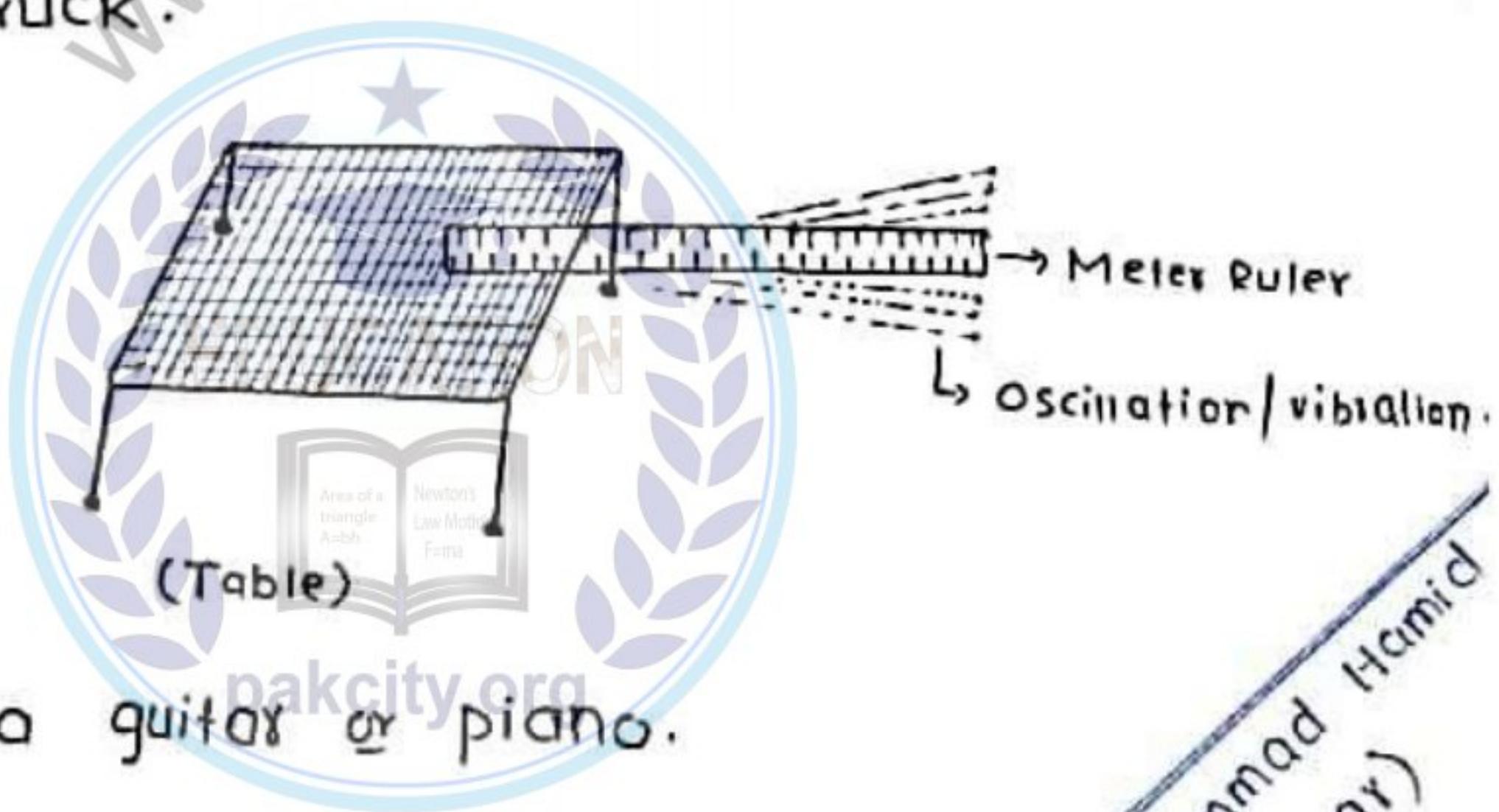


- (2) Motion of a mass attach to a Spring.

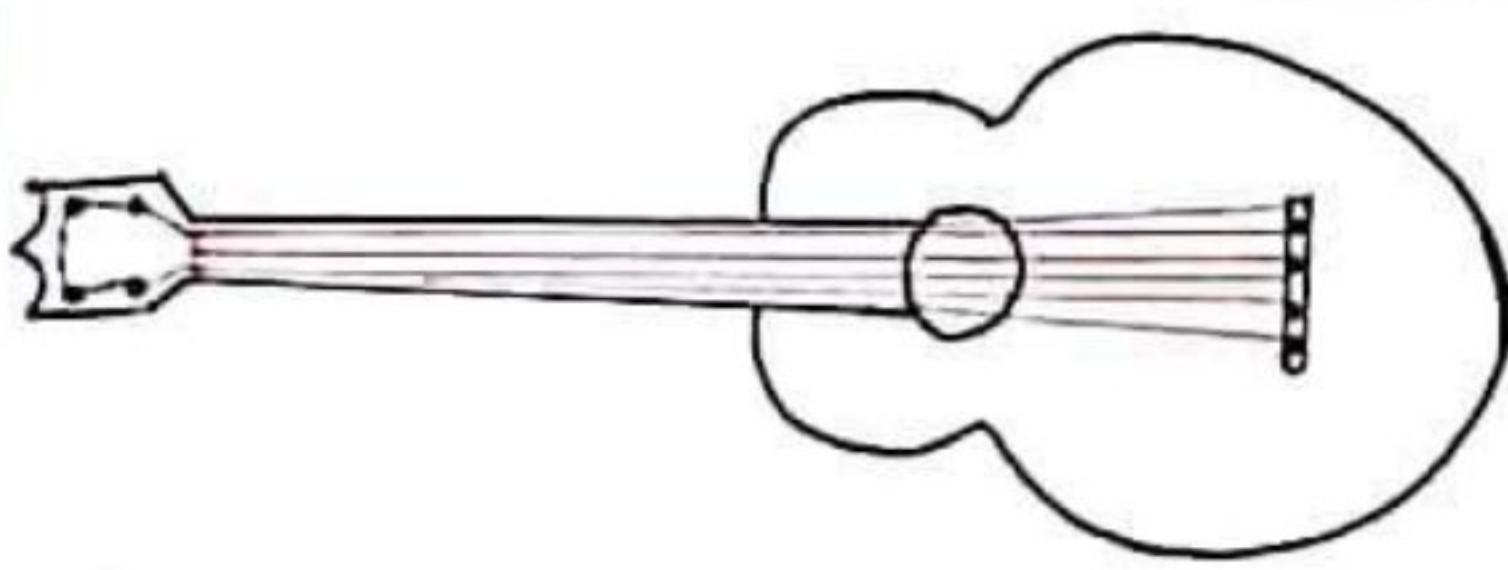


- (3)

- (4) A plastic Ruler held firmly over the edge of a table and gently STRUCK.



- (5) The String of a guitar or piano.

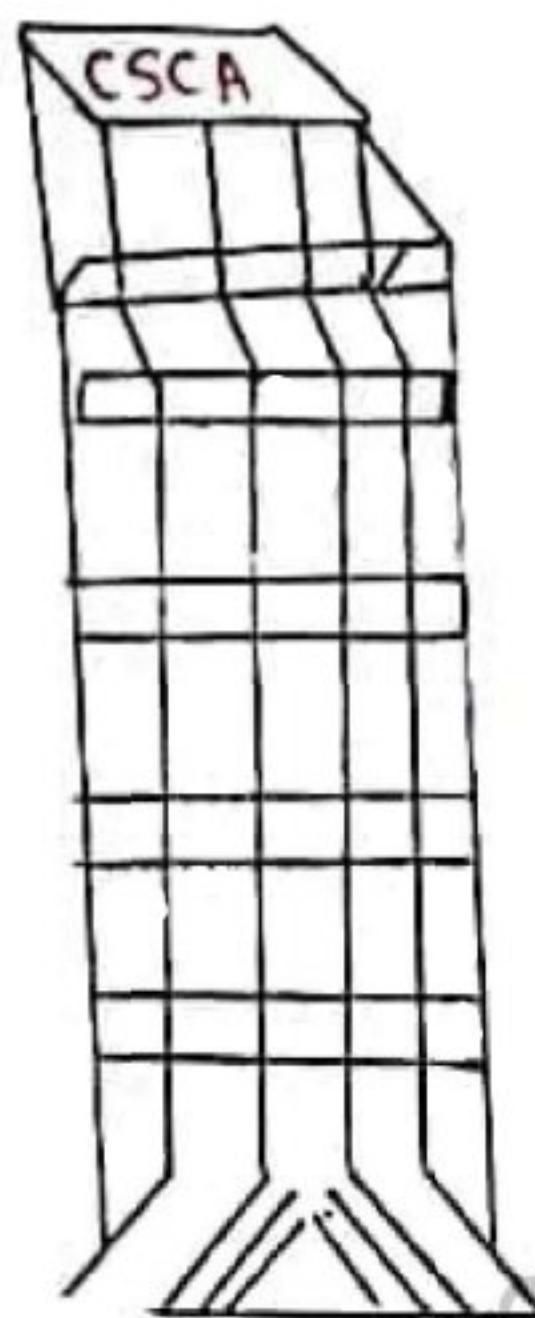


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(6) vehicles Oscillate up and down when they hit a bump.



(7) Building and bridges vibrate during an earth quack.



### Terminologies Of Oscillatory motion:

A) **Cycle/vibration:** " One Complete round trip of vibrating body about Certain Equilibrium position is Called Cycle or vibration.

#### Explanation:

Consider a Simple pendulum as shown in the figure.

Starting from point "A" and cross point "B"

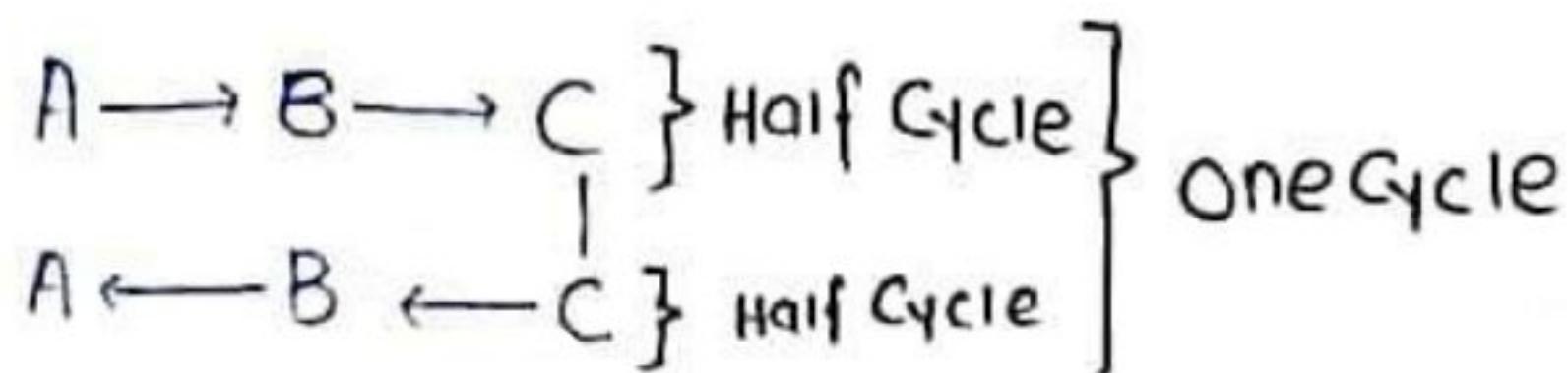
and reach point "C"

and than start back motion from point "C" and cross point "B" and reach point "A". So, this is a one



Complete rotation.

i.e



(OR)

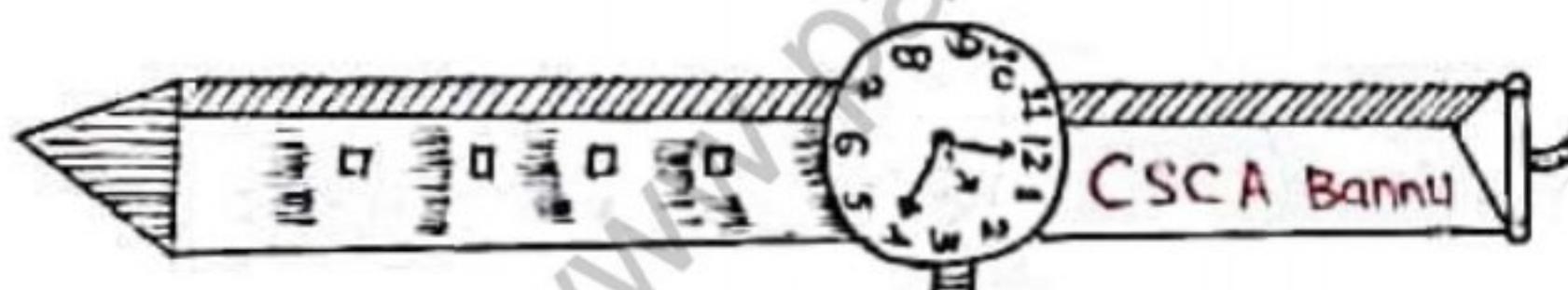


(B) Time Period: **(T):** "The time required to complete one cycle or vibration

is called time period:

① Representation: "Time period is represented by Capital 'T'"

② S.I unit: "The S.I unit of time period is second."



(C) Frequency: **(f):** "The number of cycles that the particle complete per unit time is called frequency(f)."

① Representation: "Frequency is represented by 'f'."

② S.I unit: "S.I unit of frequency is cycle per second (s⁻¹) or hertz (Hz)"

Note:-

$$f = \frac{1}{T} = \frac{1}{\text{second}} = \frac{1}{s} = s^{-1} = \text{hertz}$$

So,

$$f = s^{-1} \text{ or hertz (Hz)}$$

**(D) Relation Between time period (T) and frequency (f) :**

↳ Time period and Frequency are reciprocal to each other.

↓(inversely proportional)

**Formula:**

$$T = \frac{1}{f}$$

or frequency =  $\frac{1}{\text{Period}}$

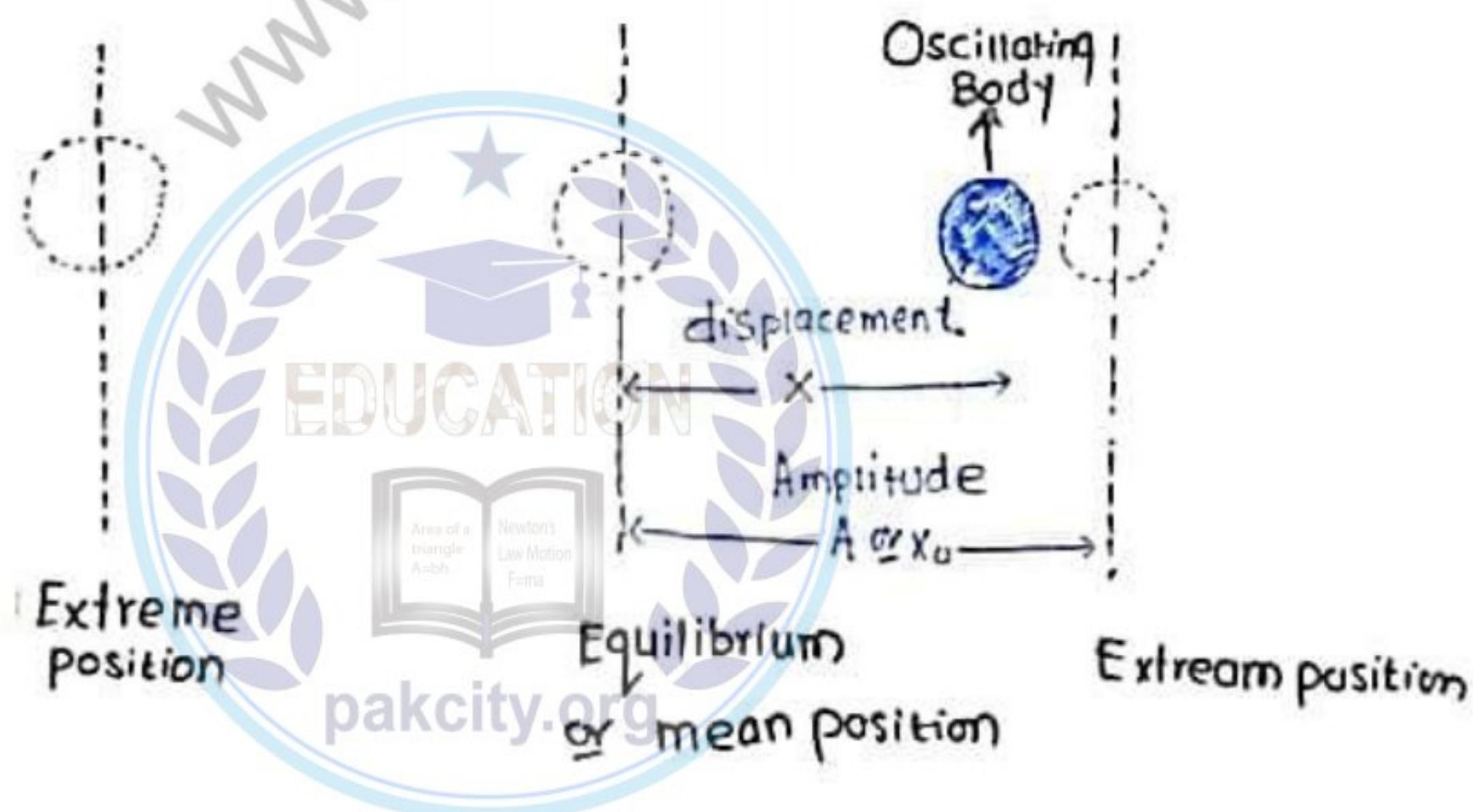
↳ if you double the period the frequency is halved

**(E) Displacement:** "The distance of oscillating body from mean position at any instant of time is called displacement."

**Representation :-** displacement is represented by "x".

**Unit :-** Displacement is measured in meter(m).

**Figure :-**



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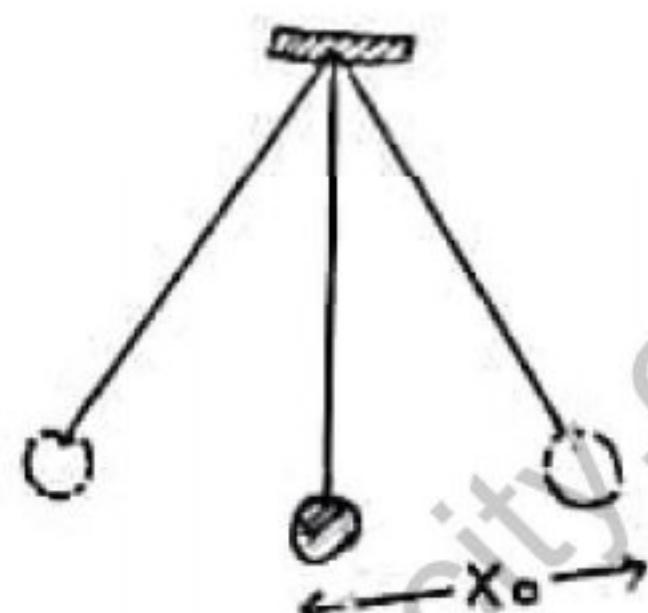
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**(F) Amplitude ( $A \text{ or } x_0$ ):** "The maximum displacement of the body from its mean position in a cycle is called amplitude ( $x_0$ ). Amplitude being a length, is measured in meter (m).

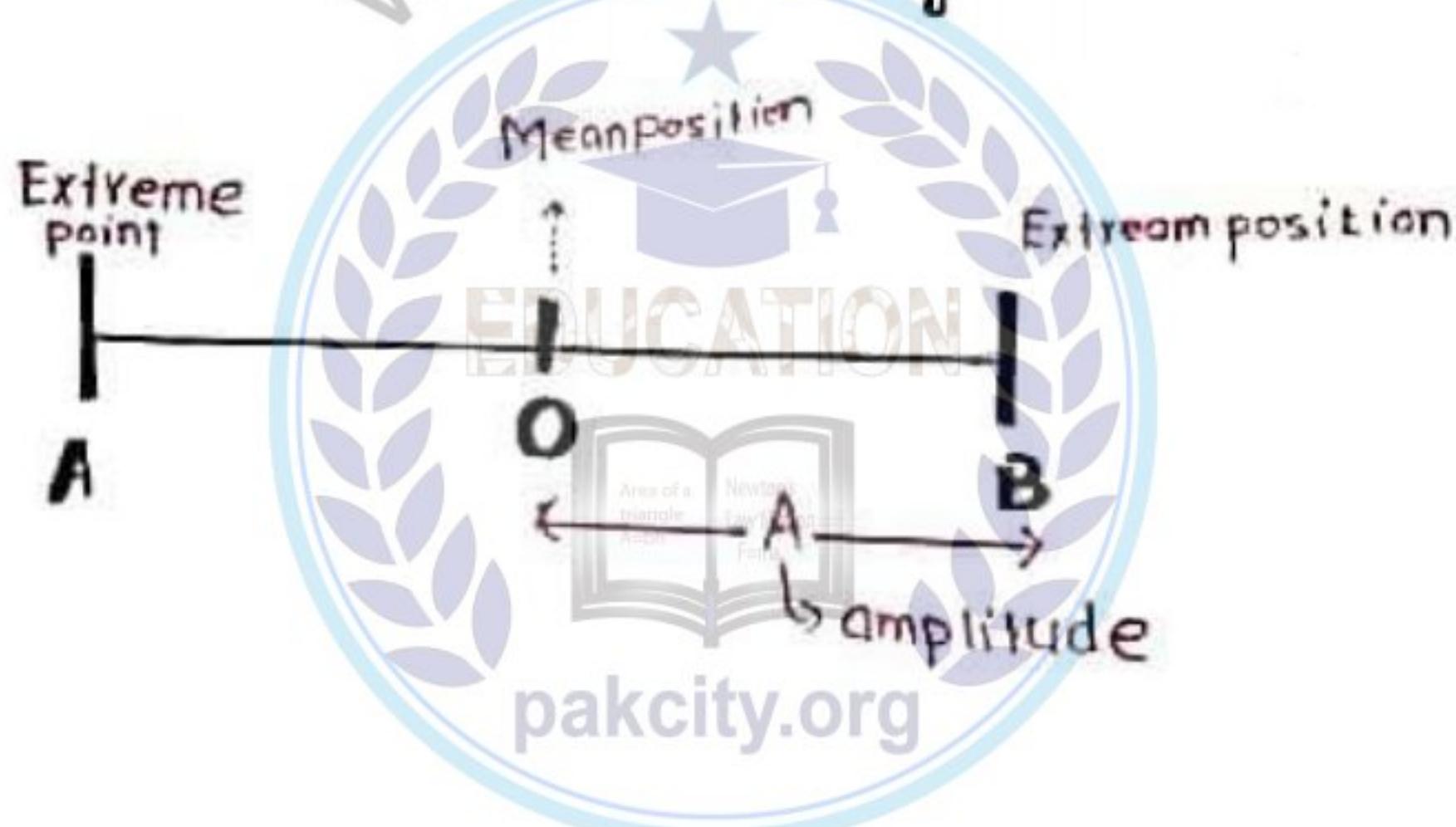
**Representation:-** amplitude is represented by  $A \text{ or } x_0$ .

**Unit of amplitude:** "Amplitude is being a length so, its unit is meter (m).

**Figure:**



**in waves:-**



## Difference Between

(1) Period Motion:

(2) Oscillation Motion:

(3) Simple Harmonic Motion:

(1) **Periodic Motion:** "A motion repeats itself after an equal interval of time is called periodic motion."

Main points: (1) There is no equilibrium position.  
 (2) There is no restoring force.  
 (3) There is no stable equilibrium position.

**Example:-** Uniform Circular motion.

(2) **Oscillation Motion:** "To and fro motion of a particle a mean position is called an oscillatory motion. In oscillatory motion a particle moves on either side of Equilibrium (or) mean position is an oscillatory motion."

Main points:- (1) It is a kind of periodic motion bounded between two extreme points

(2) The object will keep on moving between two extreme points about a fixed point is called mean position or equilibrium position along any path. (the path is not constraint).

- (3) there will be a restoring force directed towards equilibrium position (or) mean position.
- (4) in an oscillatory motion, the net (total) force on the particle is zero at mean position (equilibrium position).
- (5) Mean position in Simple harmonic Motion is stable equilibrium.



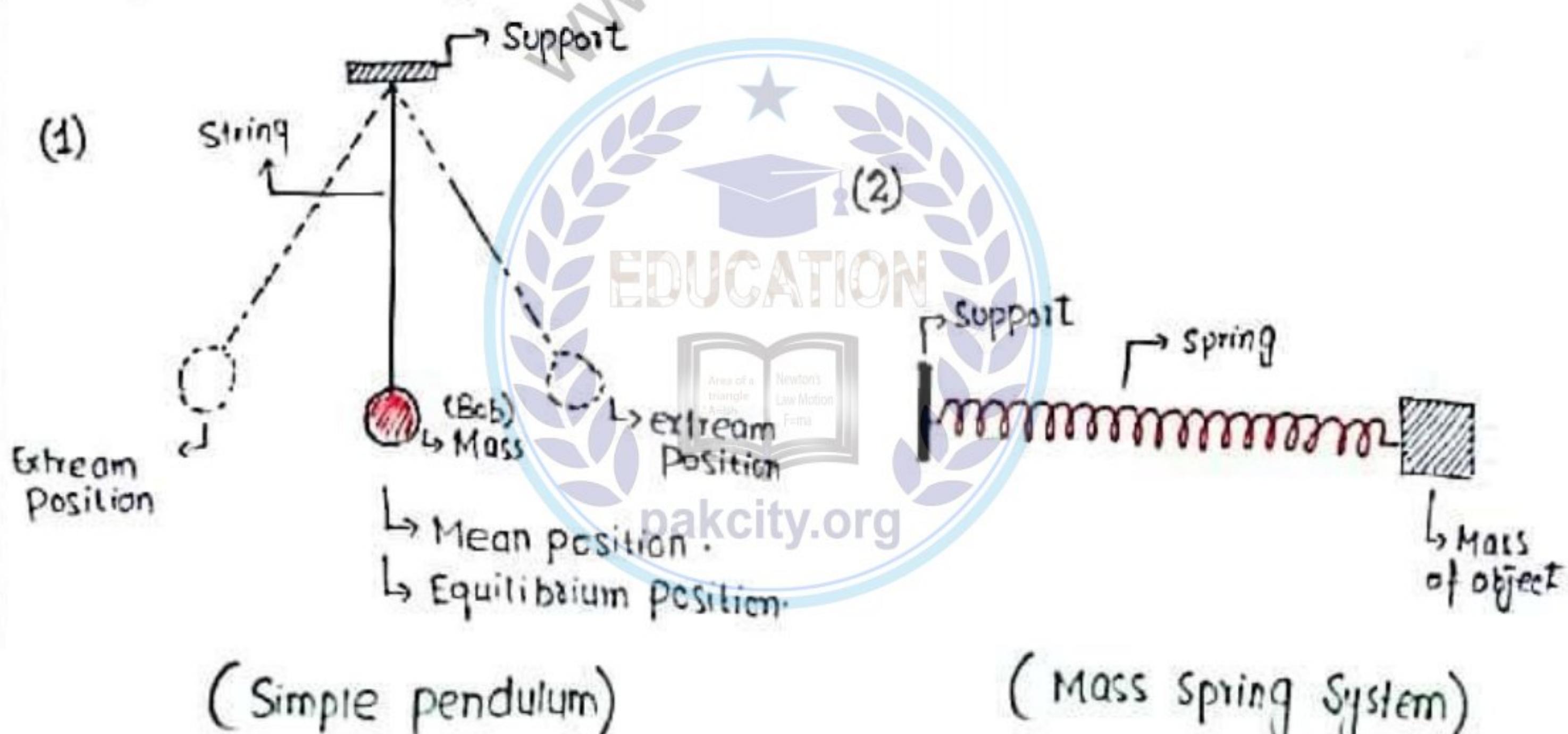
## Condition for SHM:

$$\textcircled{1} \quad \vec{F} \propto -\vec{x}$$

$$\textcircled{2} \quad \vec{a} \propto -\vec{x}$$

## Example of Simple Harmonic Motion:

- ① Oscillation of Simple pendulum  
 ② Mass - Spring System.



## Simple Harmonic Motion (S.H.M)

**Definition:** Such Type of motion in which object Performe Periodic motion under the influence of Restoring force is Called Simple Harmonic Motion (S.H.M).

.....OR.....

"A Special oscillatory motion in Which restoring force is directly proportional to the Displacement ( $x$ ) of the particle from the mean or Equilibrium position.

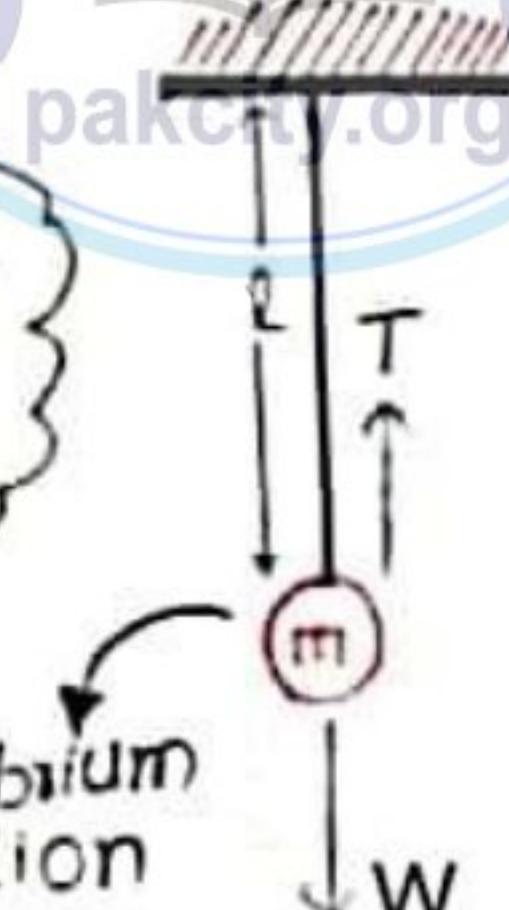
i.e.  $F_{res} \propto -x$   

$$F_{res} = -Kx$$

**Explanation:-** vibration or oscillation is repeated Back and Forth motion along the Same path. vibration occure in the vicinity of a point of Stable equilibrium.

**Equilibrium Point:** A point at which the net force acting on the body is zero.

i.e.  
 "The Tension and weight have same megnitude but opposite direction So, net force is equal to zero." Equilibrium position

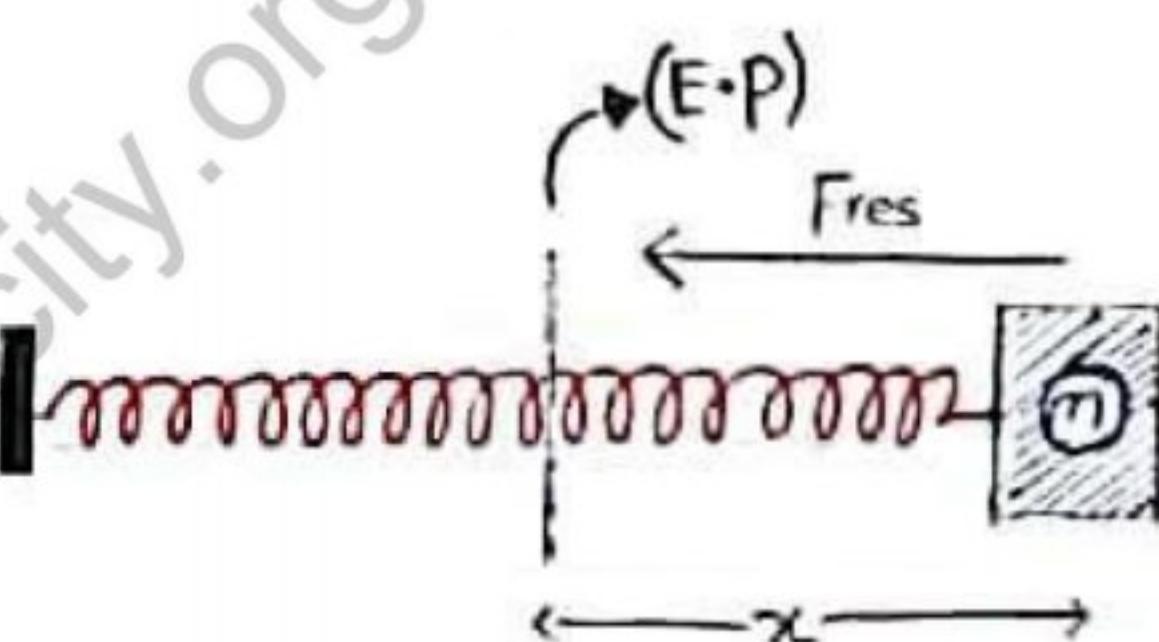
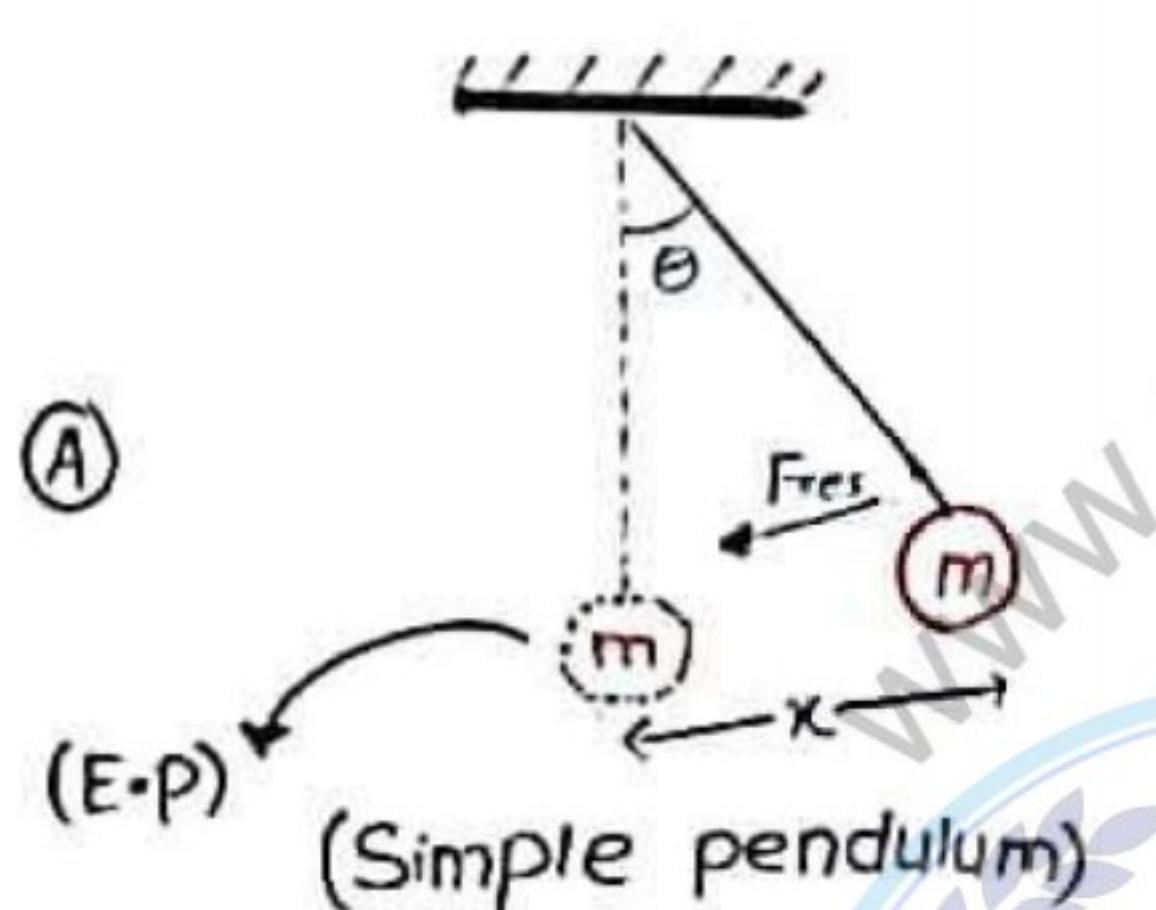


$$\begin{aligned} F_{net} &= w + (-T) \\ F_{net} &= w - T \\ F_{net} &= 0 \end{aligned}$$

→ An equilibrium point is also called Stable point. When a body is displaced from mean position by any external force ( $F_{ext}$ ) to some extreme position. then the net force pushes the body back to the equilibrium position. Such a force is called Restoring Force ( $F_{res}$ ).

**Restoring Force ( $F_{res}$ )**: " Restoring Force is a Force ( $F_{res}$ ) is a Force in oscillating System that always points toward the equilibrium position.

**Diagram:-**



∴ E.P = Equilibrium position

→ Simple Harmonic Motion obeys two conditions.

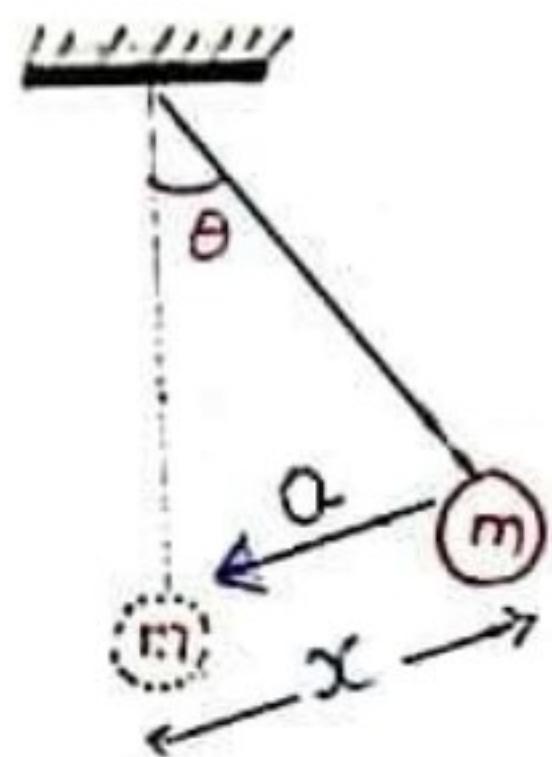
$$\textcircled{1} \quad F_{res} \propto -x$$

the restoring force is directly proportional to the displacement but Opposite in direction. Here the negative sign shows that restoring force is opposite to displacement.

\textcircled{2}

$$a \propto -x$$

the acceleration is directly proportional to the displacement.



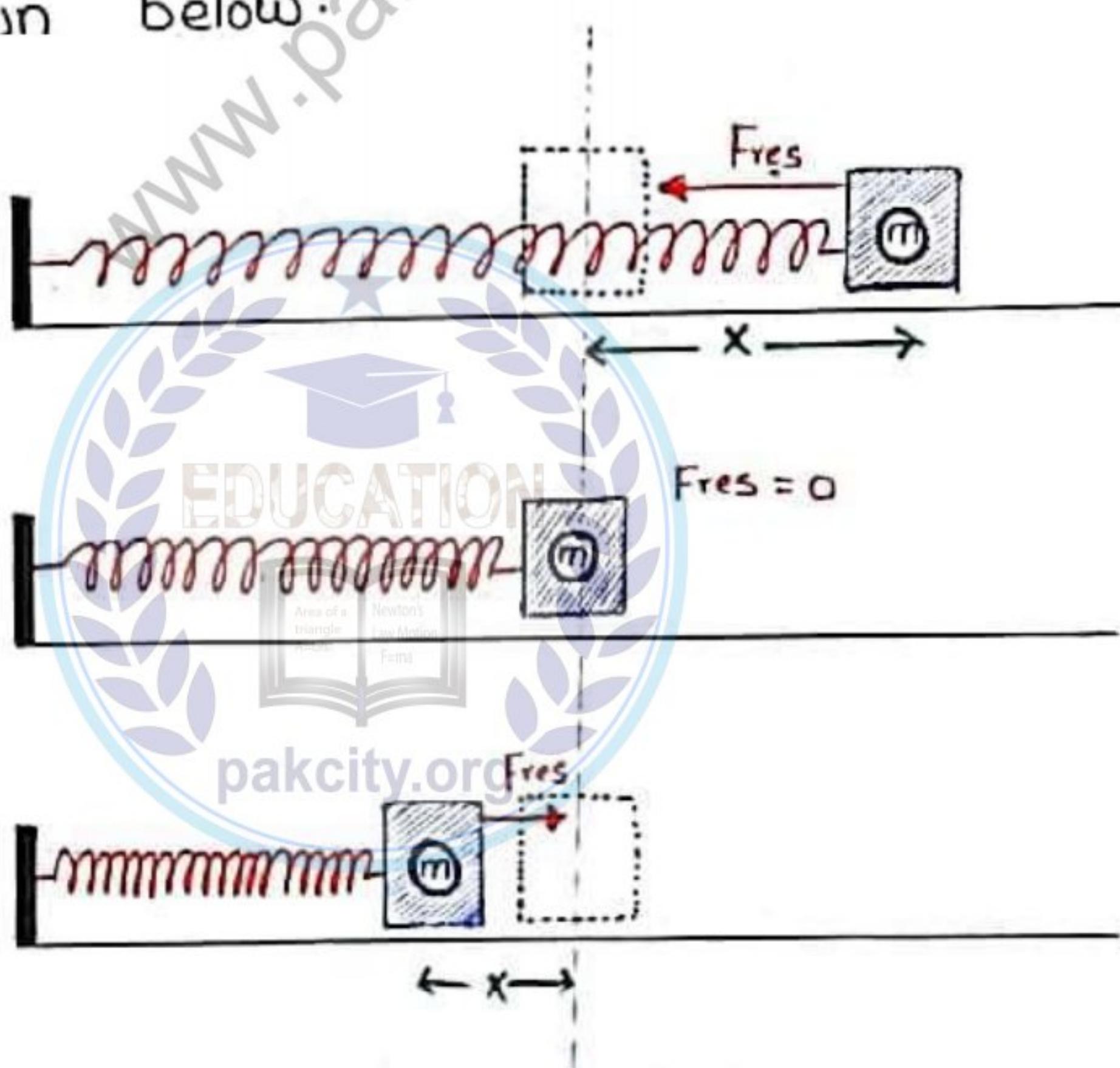
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GMP

## Motion of Mass Attached to A Spring

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Consider a block of mass ( $m$ ) attached to one end of elastic Spring which can move freely on a Frictionless horizontal surfaces as shown below.



when the block is displaced from equilibrium position to extreme position then elastic restoring force pulls the block towards equilibrium position.

So, here  $F_{res}$  is directly proportional to the displacement ( $x$ ) from equilibrium position.

$$F_{res} \propto -x$$

$$F_{res} = -Kx \rightarrow ①$$

**K** = Stiffness of the spring or Spring Constant



Restoring Force will produce acceleration in the body given by newton's second law of motion as

$$F_{res} = ma \rightarrow ②$$

Comparing equation (1) and equation (2) we get

$$F_{res} = F_{res}$$

$$-Kx = ma$$

Divide Both side By m

$$-\frac{Kx}{m} = \frac{ma}{m}$$

$$-\frac{K}{m}x$$

$$a = -\frac{K}{m}x$$

the Spring Constant "K" and mass "m" does not change during oscillation of mass attached to

Spring therefore they are regarded as Constants.

$$a = -\frac{k}{m}x$$

$\frac{k}{m}$  = Constants

$$a = -\text{Constants } x$$

$$a \propto -x$$

So, Mass Spring System obey Both Conditions

$$\textcircled{1} F_{\text{res}} \propto -x$$

$$\textcircled{2} a \propto -x$$

So, it is a Simple Harmonic Motion.

### Unit of Spring Constant (K):

We Know that

$$F_{\text{res}} = -kx$$

We also write as

$$F_{\text{res}} = \frac{F}{x}$$
$$k = \frac{F}{x}$$
$$k = \frac{\text{newton}}{\text{meter}}$$

$$k = \frac{\text{N}}{\text{m}} = \text{Nm}^{-1}$$

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# Time Period "T" and frequency "f" of mass Spring System.

**Calculation For Time Period (T) :-**

We know that the acceleration in SHM.

$$a = - \text{Constant } x \rightarrow * \quad \text{Here } \boxed{\text{Constant} = \frac{4\pi^2}{T^2}}$$

So, put value of Constant in equation \*

$$a = - \frac{4\pi^2}{T^2} x \rightarrow ①$$

We also know that

$$a = - \frac{k}{m} x \rightarrow ②$$

Comparing equation ① and equation ②

$$\begin{aligned} a &= a \\ - \frac{4\pi^2}{T^2} x &= - \frac{k}{m} x \end{aligned}$$

Cancel same Terms From both side

$$\cancel{- \frac{4\pi^2}{T^2} x} = \cancel{- \frac{k}{m} x}$$

$$\frac{4\pi^2}{T^2} = \frac{k}{m}$$

By Cross multiplication

$$\frac{4\pi^2}{T^2} = \frac{K}{m}$$

$$T^2 \times K = 4\pi^2 \times m$$

$$T^2 K = 4\pi^2 m$$

Divide Both side By "K"

$$\frac{T^2 K}{K} = \frac{4\pi^2 m}{K}$$

$$T^2 = 4\pi^2 \frac{m}{K}$$

Take square root on Both side

$$\sqrt{T^2} = \sqrt{4\pi^2 \frac{m}{K}}$$

$$T = \sqrt{4\pi^2} \sqrt{\frac{m}{K}}$$

Note

$$\sqrt{T^2} \text{ B/C}$$

$$\therefore \sqrt{T} = \frac{1}{2}$$

$$(T^2)^{\frac{1}{2}} = T$$

$$T = \sqrt{(2)^2 \pi^2} \sqrt{\frac{m}{K}}$$

$$T = \sqrt{(2\pi)^2} \sqrt{\frac{m}{K}}$$

$$T = 2\pi \sqrt{\frac{m}{K}}$$

Where:-

- $m$  = mass  $\rightarrow$  (kg)
- $K$  = Spring Constant ( $N/m^2$ )
- $T$  = Time period (s)

Note:- Time period does not depend upon "Amplitude"  $A/x_0$

## "Calculation For Frequency"

A We Know that Frequency is Reciprocal of Time periodo.

$$f = \frac{1}{T} \rightarrow \textcircled{A}$$

Put  $T = 2\pi\sqrt{\frac{m}{k}}$  in equation  $\textcircled{A}$

$$f = \frac{1}{2\pi\sqrt{\frac{m}{k}}}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$



## SIMPLE PENDULUM:-

DEFINITION:- " The Simple Pendulum is Mechanical System that moves in an oscillatory motion.

(OR)

A Simple pendulum is a device where its point mass is attached to a Light inextensible string and Suspended from a fixed point.

IDEALIZED MODEL: " A Simple pendulum is an idealized model Consisting of

- ↳ point Mass
- ↳ Weightless, in extensible string
- ↳ Supported From a Fixed Frictionless Supported

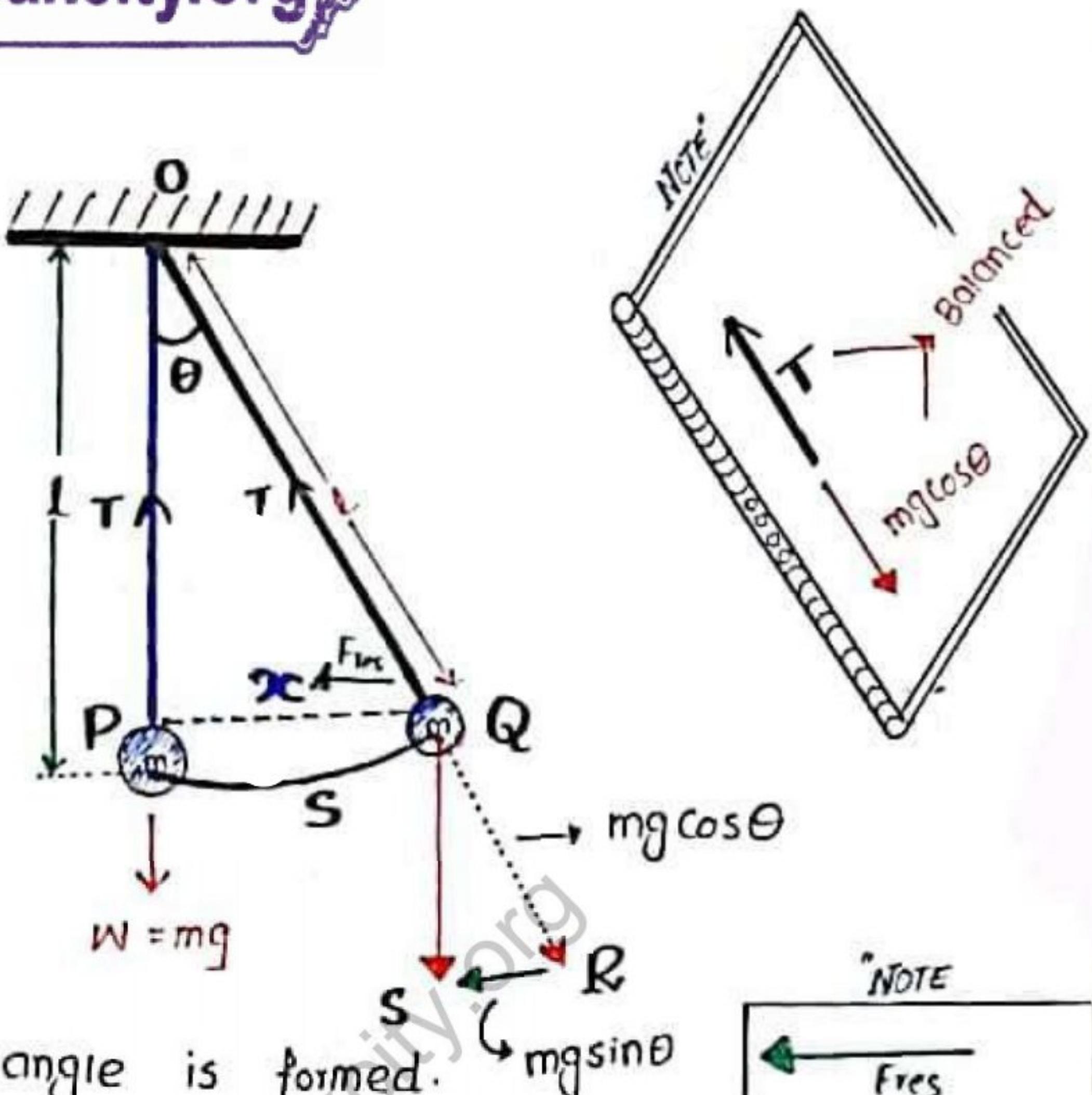
REAL MODEL:- " A Real model (pendulum) approximates a simple pendulum if

- ↳ The bob is small Compare with the length ( $l$ ).
- ↳ Mass of the string is much less than the bob's mass
- ↳ the Cord or string remains straight and does not stretch.

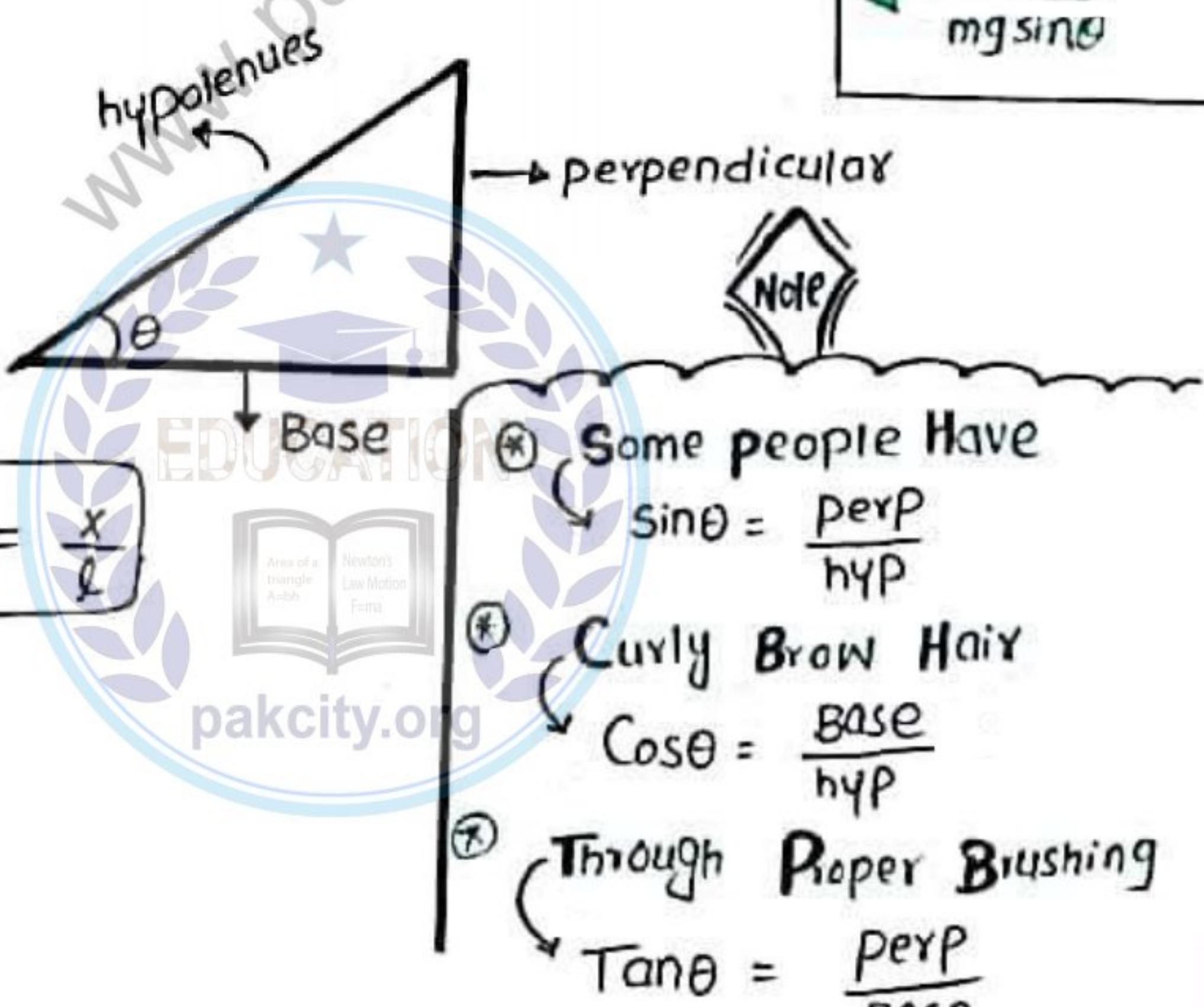
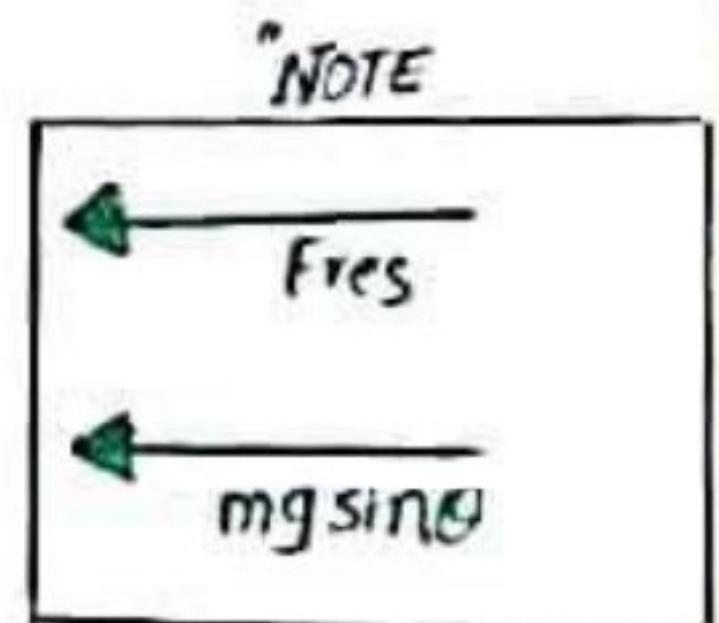
Construction OF Simple Pendulum:- Consist of

- ↳ point Mass ( $m$ )
- ↳ inextensible string of Length ( $L$ )
- ↳ Fixed Support .

## DIAGRAM:



Here a triangle is formed.



$$\sin \theta = \frac{\text{perp}}{\text{hyp}} = \frac{x}{l}$$

**EXPLANATION:** " Pull the pendulum From Mean position To extream position By using external Force ( $F_{ext}$ ). When you leave the pendulum it will move toward mean position and due to inertia it will not stop at equilibrium position and will start oscillatory motion.

→ the motion occure in a vertical plane and it driven By Gravitational Force. For  $\Delta QRS$  we resolve The weight( $w$ ) into **TWO Components**.

$$\textcircled{1} \ mg \cos\theta$$

$$\textcircled{2} \ mg \ sin\theta$$

in Figure above we note that the component  $mg \cos\theta$  Balanced By The **Tension (T)** in the string. The **Restoring Force** is only provided by the second Component  $mg \sin\theta$ : Therefore we can write as

$$F_{res} = -mg \sin\theta \rightarrow \textcircled{1}$$

→ ALSO note that in The Figure The only for Small angles The arc length "S" is nearly equal to Displacement ' $x$ '

Therefore from  $\Delta OPG$

$$\sin\theta = \frac{x}{l} \rightarrow \textcircled{2}$$

putting Equation  $\textcircled{1}$  in equation  $\textcircled{2}$  we get

$$F_{res} = -mg\left(\frac{x}{l}\right) \rightarrow \textcircled{3}$$

Here

$F_{res}$  = Restoring Force

$m$  = Mass of a bob

$g$  = Acceleration due to gravity

$x$  = Displacement

$l$  = Length of string.

Here  $m, g$  and " $l$ " are constant for simple pendulum oscillating with small angle. Therefore

$$F_{res} = - \frac{mg}{l} x$$

• Constants =  $\frac{mg}{l}$

$$F_{res} = - \text{Constants}(x)$$

$F_{res} \propto -x$  → ③

Constant Change  
to proportionality

→ This is 1st Condition of motion which is satisfied.

Simple Harmonic

According to Newton's Second LAW OF motion.

$$F = ma$$

$F_{res} = ma$  → ④

Comparing equation ③ and ④

$$\begin{aligned} F_{res} &= F_{res} \\ -mg \frac{x}{l} &= ma \\ -g \frac{x}{l} &= a \end{aligned}$$

$$a = -\frac{g}{l} x$$

Here again " $g, l$ " are constants.

$$a = -\text{Constant}(x)$$

$$a \propto -x \rightarrow \textcircled{*}$$

$$\therefore \text{Constant} = \frac{g}{l}$$

This is the 2<sup>nd</sup> Condition for S.H.M.

So, This proves that the motion of Simple pendulum is S.H.M.

### Time period "T" and Frequency "f" of Simple pendulum.

① Time period (T) :- "The Time taken by a body to Complete one cycle." it can be shown that the acceleration and displacement of a simple pendulum are related by Time period(T).

$$a \propto -x$$

$$a = -\text{Constant}(x) \rightarrow \textcircled{\ast}$$

$$\text{Constant} = \frac{4\pi^2}{T^2}$$

put the Constant value in eq  $\textcircled{\ast}$

$$a = -\frac{4\pi^2}{T^2} x \rightarrow \textcircled{1}$$

in previous topic we see that

$$a = -\frac{g}{l} x \rightarrow \textcircled{2}$$

Comparing eq  $\textcircled{1}$  and eq  $\textcircled{2}$  we get

$$a = a$$

$$-\frac{4\pi^2}{T^2} x' = -\frac{g}{l} x'$$

$$\frac{4\pi^2}{T^2} \cancel{r} = \frac{g}{l}$$

By Cross Multiplication

$$= T^2 \times g = 4\pi^2 \times l$$

$$= T^2 g = 4\pi^2 l$$

= Divide Both side By "g"

$$= \frac{T^2 g}{g} = \frac{4\pi^2 l}{g}$$

$$= T^2 = 4\pi^2 \frac{l}{g}$$

= Taking square ROOT on Both side ( $\sqrt{\cdot}$ )

$$= \sqrt{T^2} = \sqrt{4\pi^2 \frac{l}{g}}$$

$$= T = \sqrt{4\pi^2} \sqrt{\frac{l}{g}}$$

$$= T = \sqrt{(2)^2 \pi^2} \sqrt{\frac{l}{g}}$$

$$= T = \sqrt{(2\pi)^2} \sqrt{\frac{l}{g}}$$

$$= T = 2\pi \sqrt{\frac{l}{g}}$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

- ↳ Time period directly depend upon Length (l) of Pendulum and inversely on the gravitational acceleration (g)
- ↳ Time period does not depends upon mass (m) & amplitude ( $x_0/A$ ) of a pendulum.

## B) Frequency of simple Pendulum:-

Since we know that Frequency is Reciprocal of Time period.

$$f = \frac{1}{T} \rightarrow \textcircled{*}$$

Put  $T = 2\pi\sqrt{\frac{l}{g}}$  in equation  $\textcircled{*}$

$$f = \frac{1}{2\pi\sqrt{\frac{l}{g}}}$$

$$f = \frac{1}{2\pi} \times \sqrt{\frac{g}{l}}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{g}{l}}$$

## DAMPING:-

DEFINITION: "Any EFFECT That Tends (لیکھ کر) to reduced The amplitude of vibration is Called damping."

Damping Force: "A Particular Type of Force used To slow down or stop a motion, is Called damping force."

- A Force that restricts vibration that can be mechanical , or electrical in nature.

## Explanation:

ideal System" If we consider oscillatory motion for an ideal System that is , System that Oscillate indefinitely Under the

action of a Linear Restoring Force.

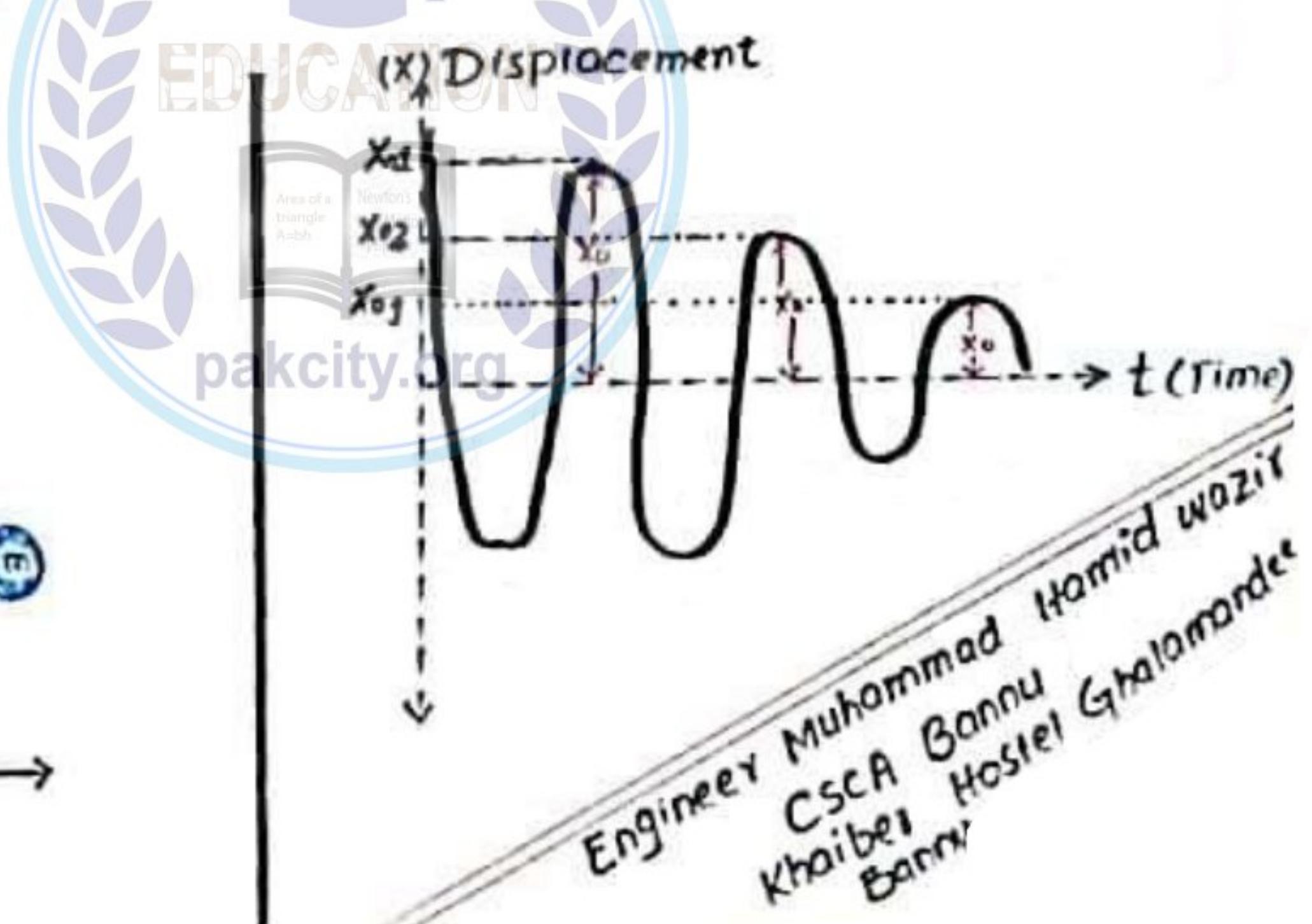
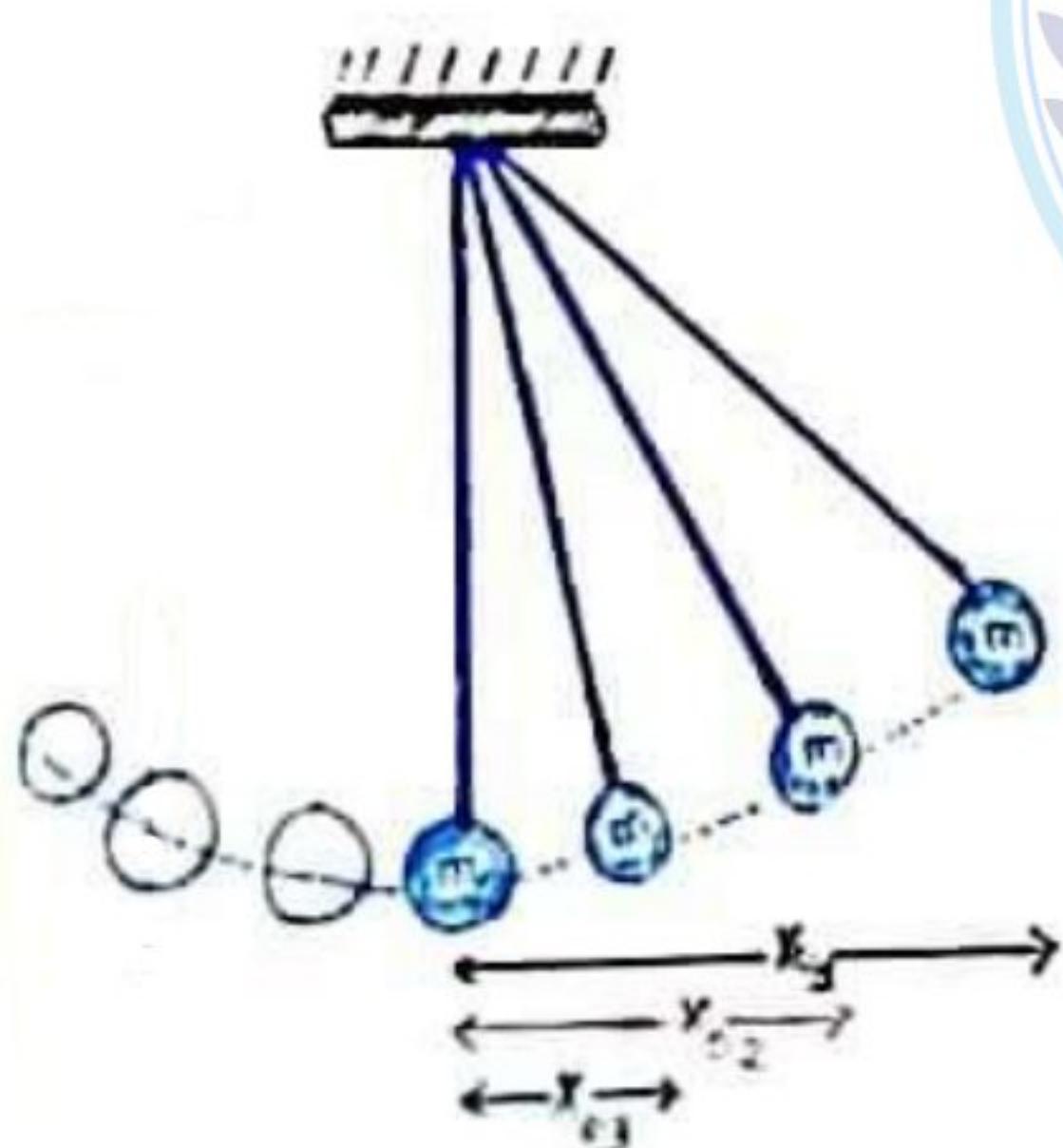
**Real System:** "However in many real System Resistive Forces such as Friction reduce the motion."

**Result:** As a result that resistive force reduce the amplitude of system progressively with Time, and the motion is said to be damped.

**Aim of Damping Force:** The aim of any damping force in an oscillatory system is to decrease the amplitude of its oscillation or prevent the oscillation from happening.

**in Pendulum:** "The motion of pendulum eventually stop if it is left untouched B/c the pendulum loses Energy by doing work on the surrounding forces, Such air resistance and friction. The energy of the system decreases with time and eventually fall to zero and pendulum comes to rest."

**Diagram:-**



# Nature OF Waves and their Types:

WAVE: " a disturbance that moves from its point of origin Transferring energy by means of vibration.

...-(OR)-...

A wave is a disturbance in a medium that carries energy without a net movement of particles.

## Common Feature to all Waves:

There are two Common feature to all Waves.

1: A wave is a traveling disturbance.

2: A wave carries energy from place to place.

Explanation: " A wave is disturbance that transfers Energy through a medium.

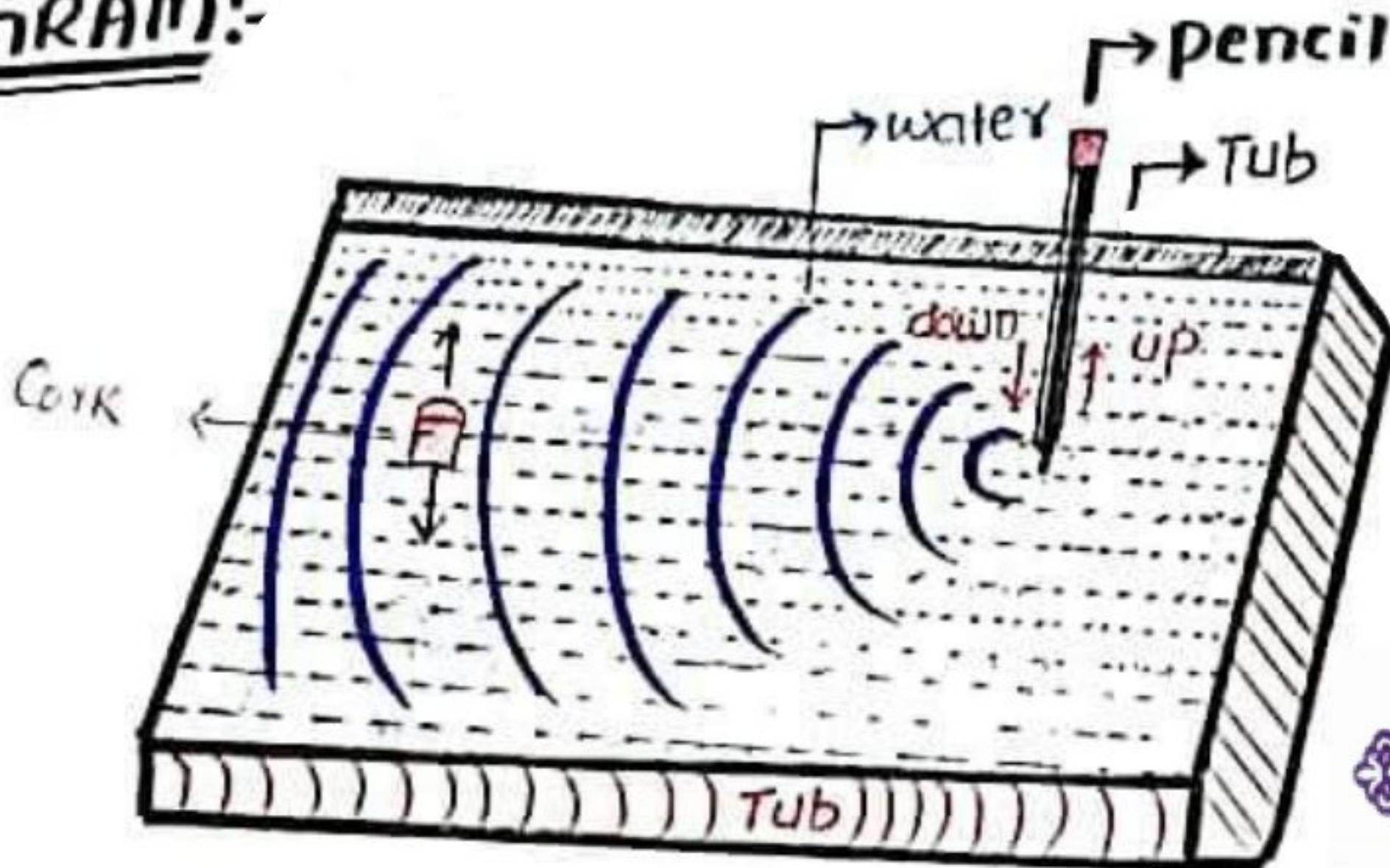
↳ Wave can't transfer matter. each particle in the medium vibrate about some mean (or rest) position as the wave passes.

## Water Waves As Means Of Energy Transfer.

Take a tub full of water moves a pencil up and down at one edge of the tub. waves are produced on the water surface which move away from point of impact of the pencil place a cork in middle of the tub. When waves moves/passes through the cork it will move up and down.

Notice that during this process the cork does not move with waves. It moves up and down which shows that the particles of matter(water) does not move forward with waves and only oscillates about mean position.

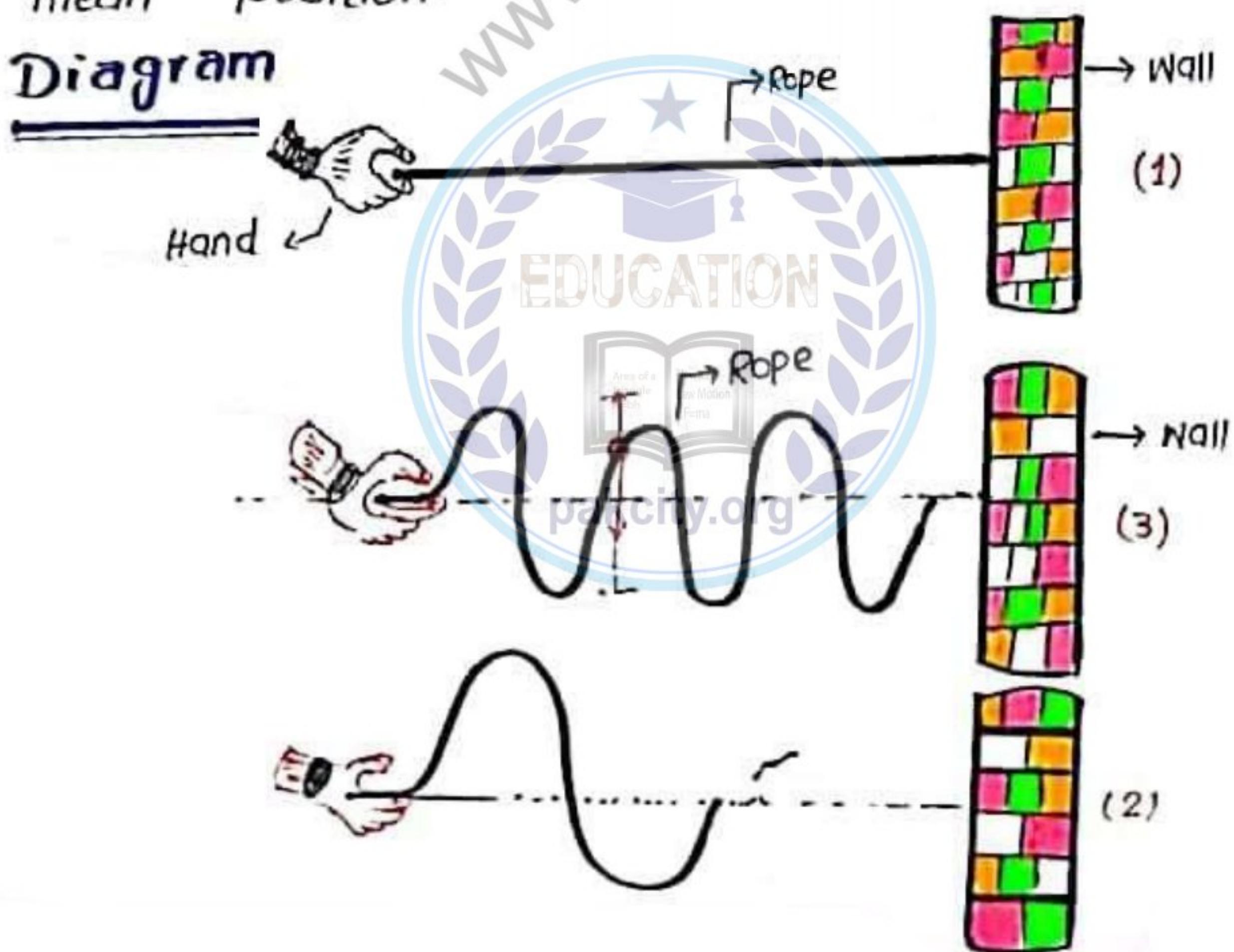
## DIAGRAM:-



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Example No2: (Rope Example): " Take a rope and Colour a part of it. attached one end of the rope to the wall and give motion up and down to the rope, regularly and Continuously. a number of waves will be produced forming a wave train. Observe The color marking. it will execute forming a wave trains. Observe the color marking. it will execute oscillation about mean position.

## Diagram

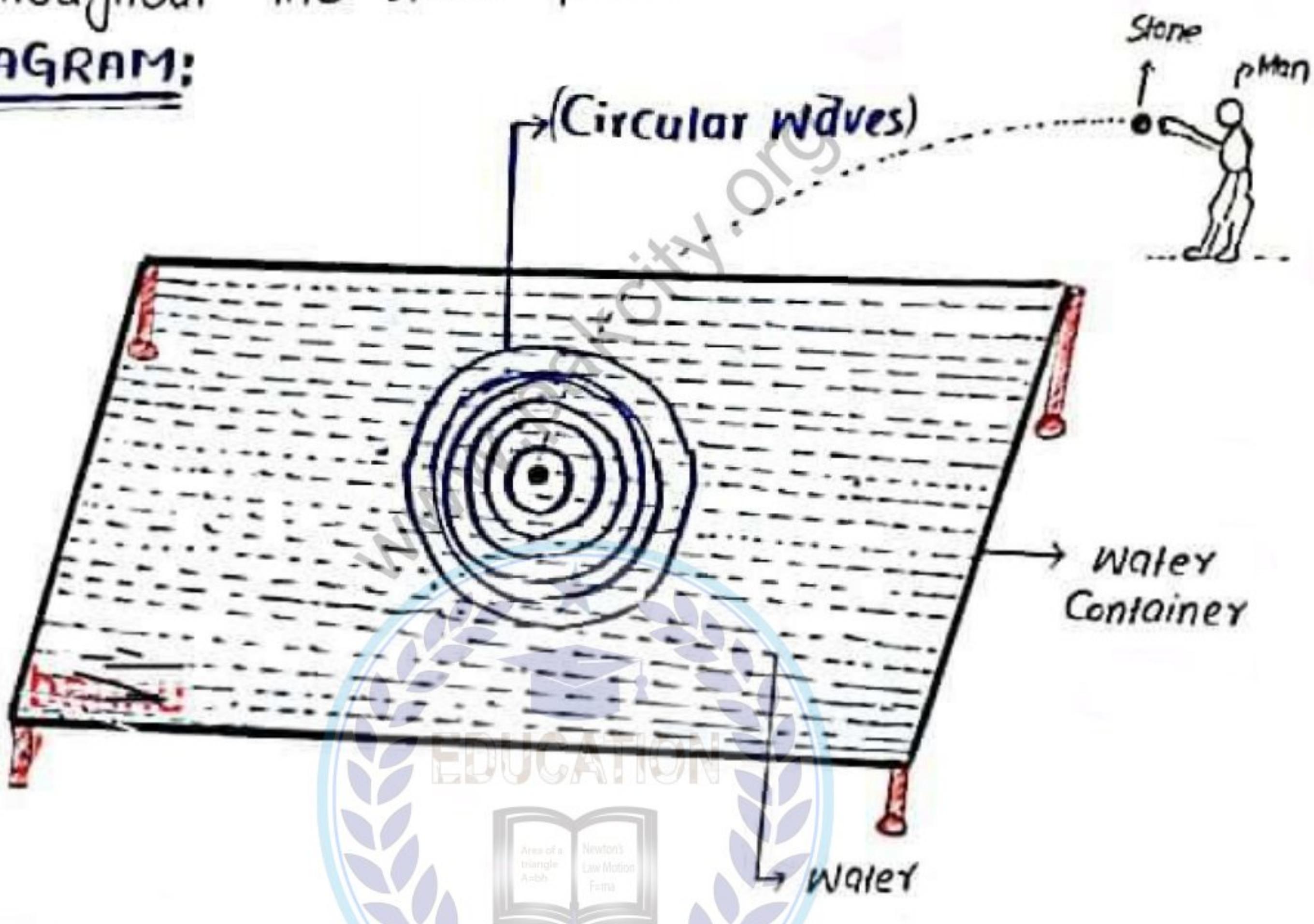


Example NO 03:

(water waves)

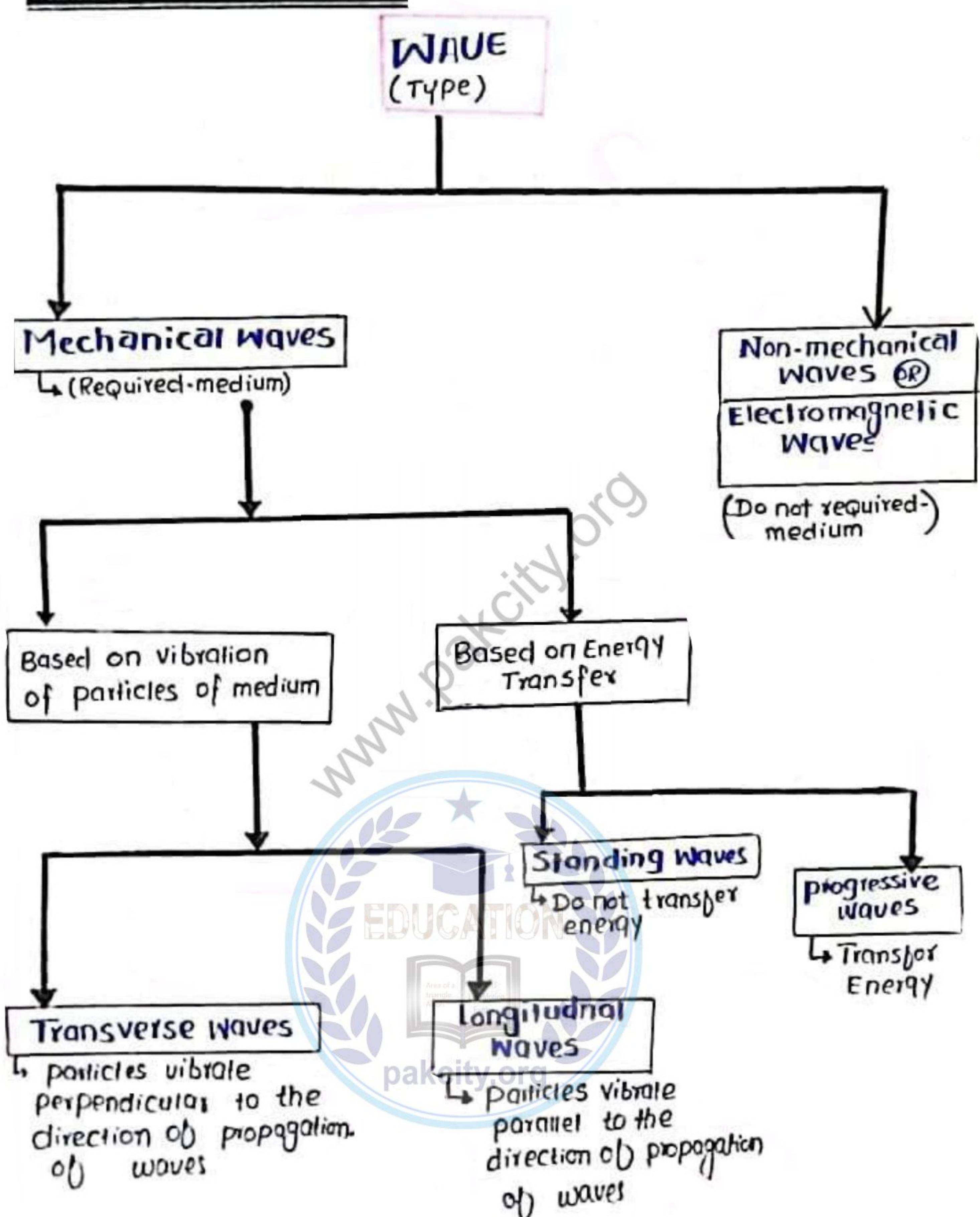
" When a stone is dropped in a pond water, ripple (waves) are produced in the pond and You will see on the surface of water. the particles of water will absorbed energy and start oscillating. these particles will transfer some of its energy to the neighboring particles which also start vibrating and all particles will start oscillating and energy is spread out throughout the water pond.

DIAGRAM:



Engineer Muhammad Hamed Wazir

## Types of Waves:



There are two categories of waves

- 1) Mechanical Waves
- 2) Electromagnetic Waves

**1) Mechanical Waves:** " waves which required medium for their propagation are called mechanical waves.

(OR)

" The waves produced by oscillation of material particles are called mechanical waves.

**Examples:**

- ① Sound waves
- ② Water waves
- ③ Air waves
- ④ Seismic waves
- ⑤ Tsunami waves
- ⑥ Waves produced on the strings and springs.

**Note:** These waves can exist only within a material medium.

**2) Electromagnetic Waves:** " Waves which do not require any medium for their propagation are called electromagnetic waves.

(OR)

" The waves that propagate by oscillation of **Electric** and **magnetic** fields are called electromagnetic waves.

E-M Waves = Electric field + magnetic Field

↳ The electric and Magnetic fields are Right Angle( $90^\circ$ ) to each other.

Examples:

- ① Radio waves
- ② Television waves
- ③ X-Rays
- ④ Heat and Light waves
- ⑤ Ultraviolet Light
- ⑥ Micro waves

Types OF Mechanical waves:



Depending upon the direction of displacement of medium with respect to the direction of propagation of waves itself, mechanical waves may be classified as Longitudinal or Transverse.

A)- TRANVERSE WAVES:- A Longitudinal waves is one in which the disturbance occurs [parallel] to the Line of travel of the waves.



## Characteristic Wave Parameters:

there are many ways to describe or measure a wave. Some characteristic depend on how the wave is produced, whereas others depends on the medium through which the wave travels. Certain Characteristic wave parameter and their definition are given as under.

(1) Wavelength

(2) Amplitude

(3) Wave Cycle

(4) Frequency

(5) Time Period.

(6) Wave Speed

**(1) Wavelength ( $\lambda$ ):** "The shortest distance between points where the wave pattern repeats itself is called the wavelength."

OR

"The distance between two successive crest or trough is called wavelength. i.e. [Transverse wave]

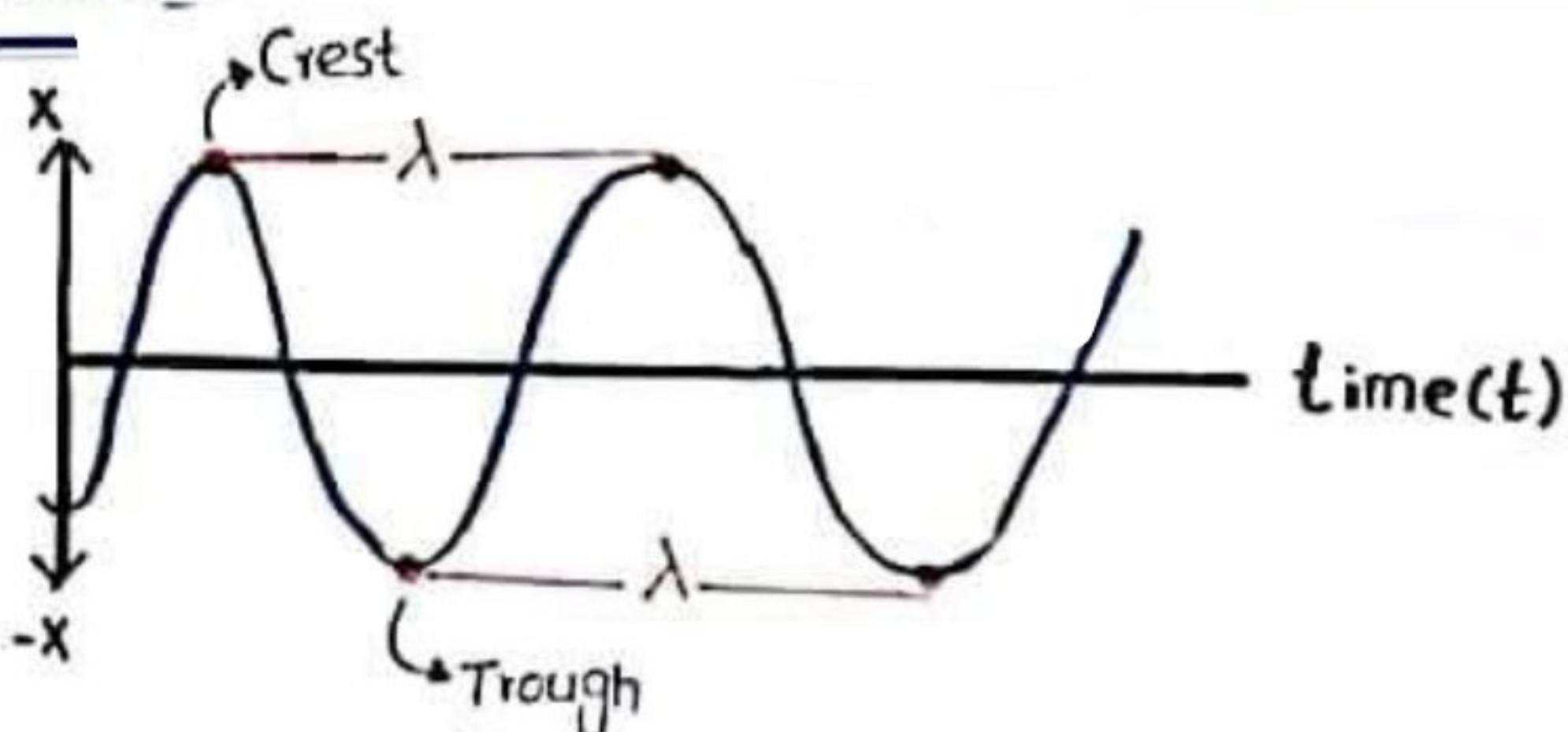
OR

"The distance between two successive compression or rarefaction is called wavelength."

**Representation:-** "represented by a Greek letter Lambda( $\lambda$ ). i.e. [Longitudinal wave]

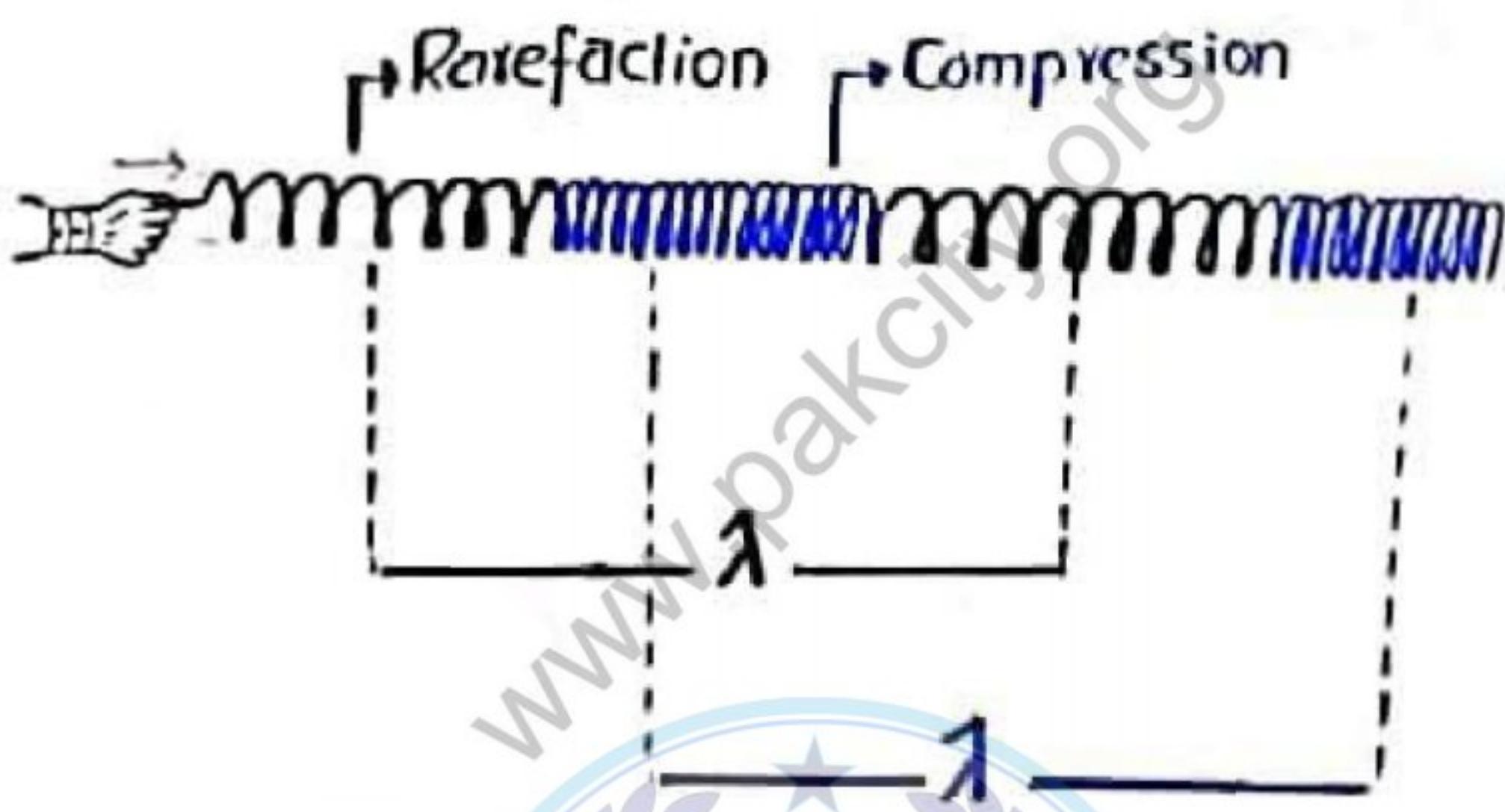
**Unit:** "The unit of wavelength is meter(m). B/c it is a distance."

### Diagram: (1)



(wavelength of transverse wave)

### Diagram No 02:



(wavelength of longitudinal waves)

\* **CREST**: "in Case of transverse wave the portion of the displacement **above** the Equilibrium position is Called Crest .

\* **TOUGH**: " in Case of transverse wave .The portion of the displacement **below** the Equilibrium position is Called Trough .

## Amplitude ( $x_0/A$ )

" Magnitude of maximum Displacement of the elements of wave from their equilibrium position is called amplitude.

(OR)

" The amplitude ( $A/x_0$ ) of a wave is the distance from the Centre line (equilibrium position) to the top of a crest or to the bottom of a trough.

(OR)

The loudness or the amount of amount of maximum Displacement of vibrating particles of the medium from their mean position is called Amplitude.

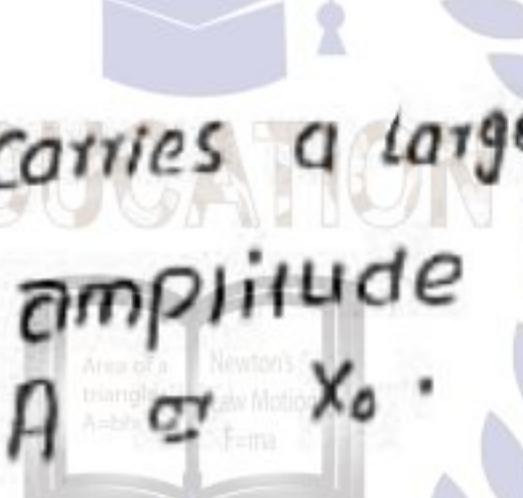
**Note:** ↳ loudness is directly proportional to amplitude of the sound. If amplitude of a is small then the sound will be feeble.

↳ the amplitude have no negative value.

↳ The amplitude of a wave is the hight of a wave.

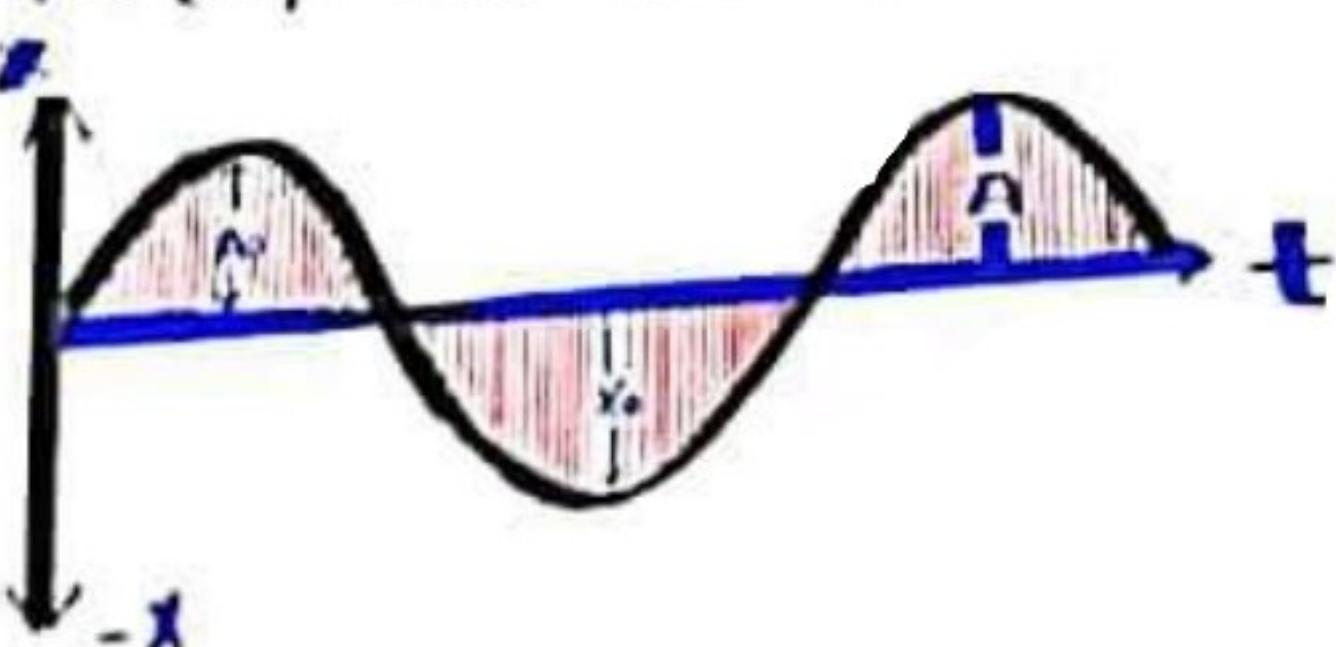
↳ A high amplitude wave carries a large amount of energy.

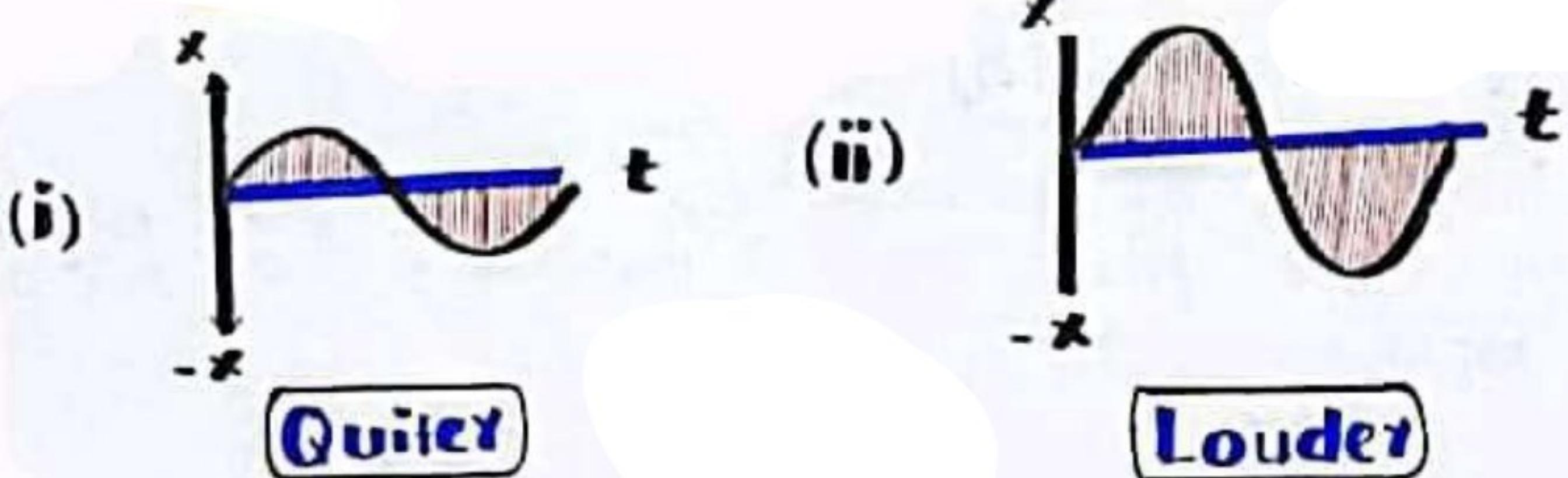
## Representation:



**Unit:** " the amplitude unit in S.I system is meter(m). B/c it is a distance.

## Diagram:



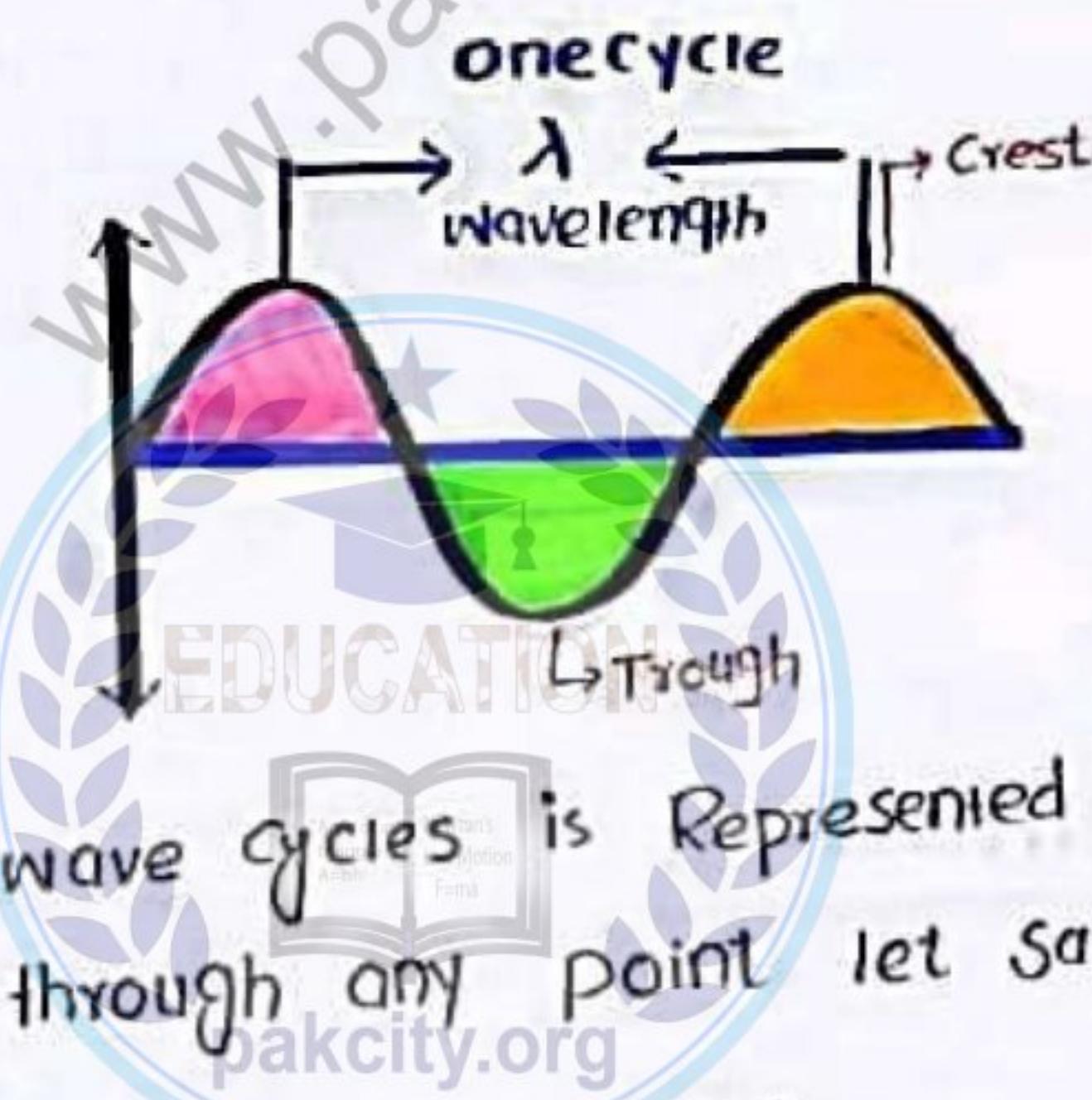


Wave Cycle: "Wave's Peak to Peak or Trough to Trough."

(OR)

one complete wave cycle is referred to as a wavelength. ~~or~~ we can say "the wavelength of a wave is simply the length of one complete wave cycle."

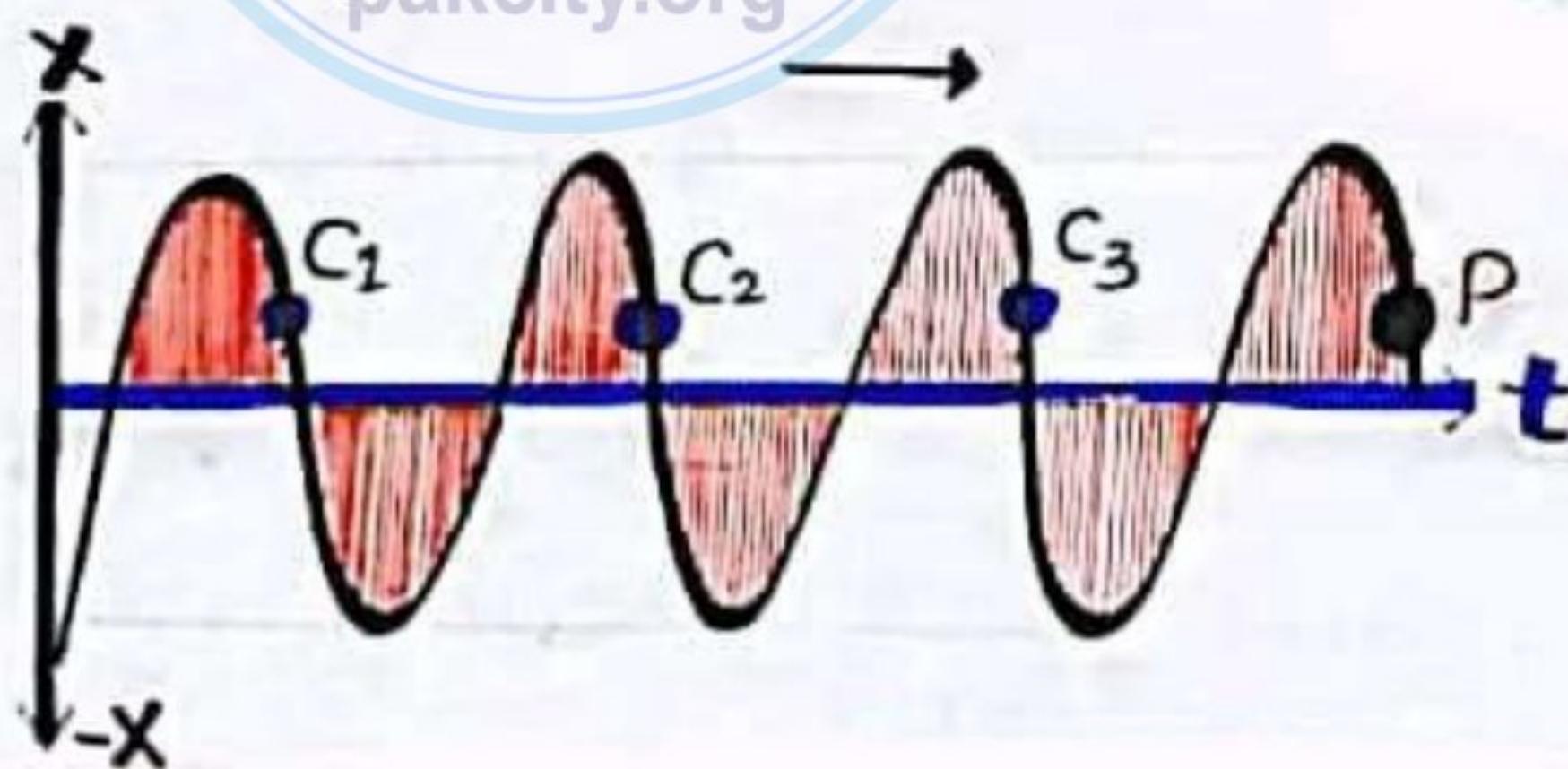
Diagram:



Available at  
www.pakcity.org

The number of wave cycles is represented by "N".  
which passes through any point let say point "P"

Diagram:-



The wave show three wave cycles  $C_1, C_2, C_3$  which are passing through a point "P".

**FREQUENCY** " $f$ " :- "The number of wave cycles (N) passing through a certain point (P) in unit time ( $t = 1$  second) is called Frequency.

(OR)



"The number of waves that pass a fixed point in a given amount of time ( $t$ ) is called Frequency of a wave."

**Representation:** "Frequency is represented by a small  $f$ :

- ↳ Also note that the frequency is also represented by a Greek letter **nu ( $\nu$ )** and **omega ( $\omega$ )**
- ↳  $\nu$  ( $\nu$ ) is used more often when specifying electromagnetic waves such as Light, X-rays, and Gamma rays.
- ↳  $\omega$  ( $\omega$ ) is usually used to describe the angular frequency that is how much an object rotates or revolves in radian per unit time.

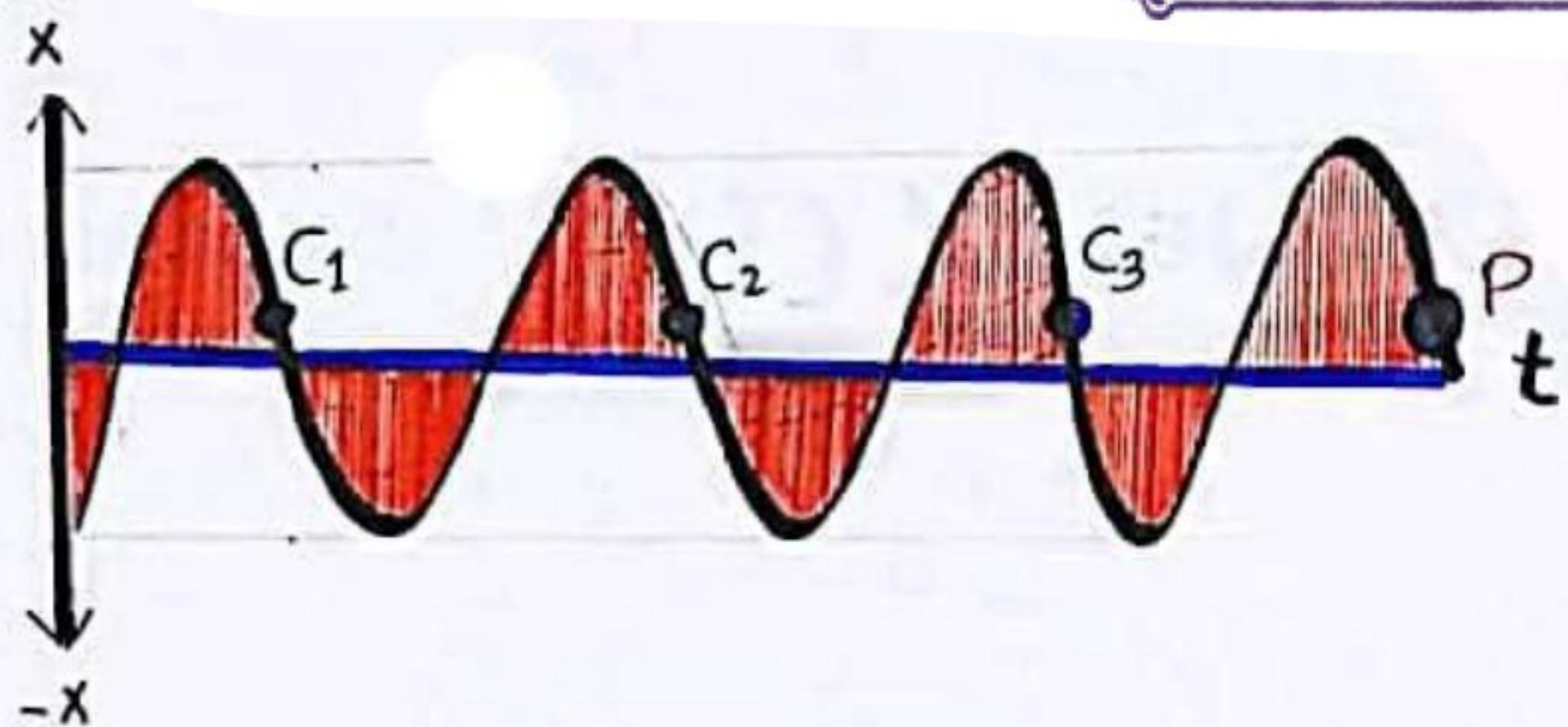
**Unit:** The S.I unit of Frequency is  $\text{hertz} (\text{Hz})$  or cycle per second ( $\frac{1}{s}, \text{s}^{-1}$ ).

**Formula:**

$$f = \frac{N}{t}$$

$\therefore f$  = Frequency  
 $\therefore N$  = No of cycle  
 $\therefore t$  = time

## Diagram:



in the above wave the number of wave cycles are three ( $C_1, C_2, C_3$ ) and if its passes through a point "P" in one second than frequency will be  $3\text{Hz}$ . i.e

$$N = 3$$

$$t = 1\text{s}$$

$$f = ?$$

$$f = \frac{N}{t} = \frac{3}{1\text{s}} = 3\text{s}^{-1}$$

$$f = 3\text{s}^{-1} \text{ or } 3\text{Hz}$$



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