### Chapter = 12

### Electrostatics

### INTRODUCTION



\*<u>Electrostatics</u>: "The branch of Physics which deals with the study of charges at rest under the action of electric force is called Electrostatics".

<u>Electric charge: "An intrinsic property of fundamental particles which takes parts in conduction process is called electric charge.</u> Either they repel or attract each other".

### Kinds of charges

There are **two** types of charge, **positive** and **negative**, charge on proton is positive and charge on electron is negative.

SI unit of charge: SI unit of charge is coulomb

How many electrons one Coulomb: 6.25x10<sup>18</sup> electrons

Electric force: The force which holds the positive and negative charges to make up atoms and molecules is called electric force.

### \*Types of electric force

Repulsive force: The force block two same charges (The force b/w two electrons)

Attractive force: The force b/w two different charges(The force b/w electron and proton)

### \*Basic law of electrostatics for knowing the nature of charge

"Like/same charges repel each other, while unlike/different charges attract each other"

### \*Q. STATE AND EXPLAIN COLOMB LAW. DISCUSS ITS VECTORIAL FORM AND GIVE EFFECT OF MEDIUM ON IT.

In 1784, French military engineer Charles Coulomb deduced a law known as Colomb law which measures the force b/w two charges.

<u>Statement:</u> "The force of attraction or repulsion b/w two charges is directly proportional to the product of the magnitude of charges and inversely proportional to the square of distance b/w them".

Mathematically: -  $F \propto q_1 q_2$  and  $F \propto \frac{1}{r^2}$  .....>  $F = K \frac{q_1 q_2}{r^2}$ 

K (Colomb Constant): K is called Colomb constant, whose value is 9\*109 Nm2C-2.

The value of K depends upon: - a) the system of units b) Nature of medium b/w charges

If medium is free space then  $K = \frac{1}{4\pi\varepsilon_o}$ ,  $\varepsilon_o$  is permittivity of free space its value in SI unit is

8.85 \* 10<sup>-12</sup> 
$$N^{-1}m^{-2}c^2$$
, so Colomb law becomes  $F = \frac{1}{4\pi\varepsilon_0} \frac{q_1q_2}{r^2}$ ,

This is mathematical form of Colomb law.

Vectorial form of Colomb law: Let us consider two point charges q1 and q2,

if  $q_1$  exert a for on  $q_2$  then  $q_2$  also exert a force on  $q_1$  which is equal in magnitude but opposite in direction as shown in fig

$$\vec{F}_{12} = \frac{1}{4\pi\varepsilon_o} \frac{q_1 q_2}{r^2} \hat{r}_{12} - - - - - (1$$

$$\vec{F}_{21} = \frac{4\pi\varepsilon_o}{4\pi\varepsilon_o} \frac{r^2}{r^2} \hat{r}_{21} - - - - (2)$$

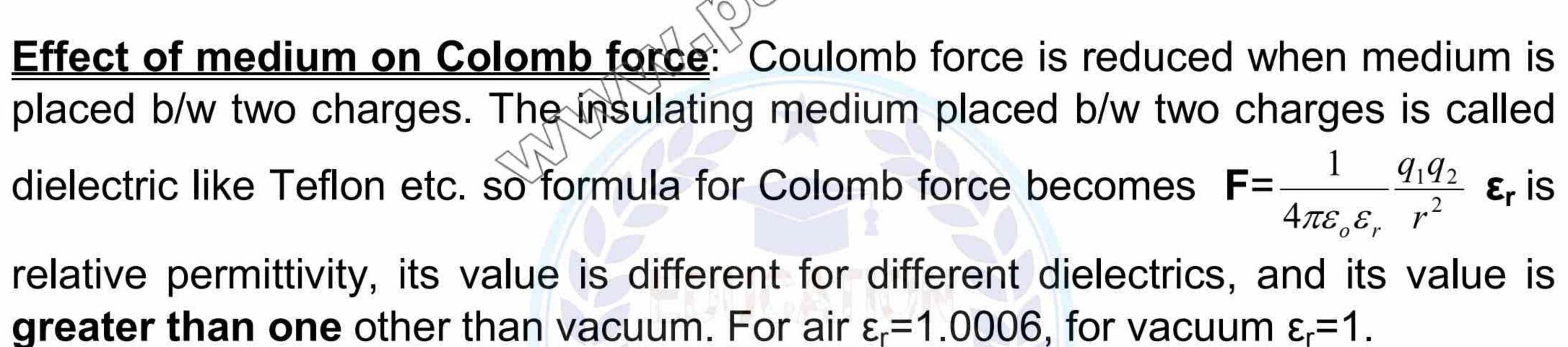
Both forces are equal but opposite in direction so

of 1m is

$$\vec{F}_{12} = -\vec{F}_{21}$$

This is called Vectorial form of Colomb Law.

this is mutual force.



Limitation of Colomb law: Colomb law is applied only on point charges.

### Multiple Choice Questions

- SI unit of Coulomb constant  $Nm^2C^{-2}$   $C^2N^{-1}m^2$   $C^2N^2m^{-2}$   $Nm^{-2}C^2$
- The electric force of repulsion 1.8N 1.5x10<sup>-9</sup> N 2.3x10<sup>-28</sup> N 2.3x10<sup>-30</sup>N between two electrons at distance
- 3 If the distance between two point Half Double Four times One charges is doubled then force between them will becomes
- 4 If the distance between two Half One fourth Two times <u>Four times</u> charges is half then force becomes

5	Two point charges +2C and +6C	Zero N	$8x10^9$	$108 \times 10^9 \text{N}$	12x10 <sup>9</sup> N
	repel each other if a charge of -2C		N(attractive)	(repulsive)	(attractive)
	is given to each of them then electric force will be				city.org
	electric force will be			B.	
6	SI unit of Eo is	$Nm^2C^{-2}$	$\mathbf{C^2N^{-1}m^{-2}}$	$C^2N^2m^{-2}$	Nm <sup>-2</sup> C <sup>2</sup>
7	The value of relative permittivity for all the dielectrics other than air or vacuum is unit:	Less than unity	Greater then unity	Equal to unity	Zero
8	Presence of dielectric other than air or vacuum always	Increase the electric force	Decrease the electric force	Does not affect electric force	Double the electric force
9	The force between two charges separated by air is 4N. When separated by a medium of relative permittivity 2. The force between them becomes	½ N	2N	4N	8N
10	Dielectric constant for Teflon is	100	2	<u>2.1</u>	2.94
11	One coulomb charge is created by	0010	$1.6 \times 10^{-19}$	$6.25 \times 10^{18}$	6.25x10 <sup>21</sup>
		electron	electron	electrons	electron
12	The force b/w two charges is 28N, if dielectric of value 2.8 is kept then force becomes	10 N	20 N	30 N	40 N
13	The value of coulomb constant in SI	6.25x10 <sup>-</sup>	8.85x10 <sup>-12</sup>	9x10 <sup>9</sup>	1.6x10 <sup>-19</sup>
14	SI unit of charge	Ampere	Volt	eV	<u>Coulomb</u>

What is Electric field and electric field intensity? Derive its formula.

\*Electric field: The space or region around a charge within which another charge experience a force is called electric field".

Michal Faraday introduced the concept of electric field.

\*Electric field intensity: @pakcity.org

"The force experience by unit positive charge placed a point in electric field is called electric field strength or field intensity", its unit N/C and formula  $\vec{E} = \frac{F}{-}$ 

it is vector quantity and its direction along the direction of force.

### \*Electric field intensity due to a point charge q:

The force experienced by test charge qo placed in the field of charge q is calculated by Colomb law and electric field intensity is calculated by putting in formula of field intensity.

$$\vec{E} = \frac{\vec{F}}{q_o} \quad -----(1)$$

$$\vec{F} = \frac{1}{4\pi\varepsilon_o} \frac{qq_o}{r^2} \hat{r} \quad --- (2 \quad \text{put this value in equation (1)}$$

$$\vec{E} = \frac{1}{q_o} * \frac{1}{4\pi\varepsilon_o} \frac{qq_o}{r^2} \hat{r} = \frac{1}{4\pi\varepsilon_o} \frac{q}{r^2} \hat{r}$$
 also written as  $\vec{E} = K \frac{q}{r^2} \hat{r}$   
Electric field intensity depends upon a) magn

Electric field intensity depends upon a) magnitude of charge b) medium c) distance from charge

What are Electric field lines? Write its properties.

<u>Definition</u>: "The direction of electric field intensity is represented by lines which are called electric field lines".

- Michal Faraday introduced the concept of field lines.
- The field due to positive point charge is directed radially outward
- The field due to negative charge is directed radially inward
- The middle region b/w two same charges has no field due to repulsion of like charges, is called zero field sport or neutral zone.

Properties of Electric field lines: There are following properties field lines

- i) Electric field lines starts from positive charges and end on negative charges.
- ii) The tangent to a field line at any point gives the direction of the electric field intensity at that point.
- iii) The lines are closer where the field is strong: the lines are farther apart where

the field is weak.

iv) No two lines cross each other because at a single point electric field has only one direction.

### PRACTICE MCQS

		FRAC	TICE WICKS		
	Concepts of electric field lines was given by	Colomb	<u>Faraday</u>	Joule	Millikan pakcity.org
2	The field created by positive charge	Radially outward	Radially inward	Both A&B	None of these
3	The field created by negative charge	Radially outward	Radially inward	Both A&B	None of these
4	The value of field at middle region b/w two same charges	Maximum	Minimum	<u>Zero</u>	None
5	The lines which provide information about the electric force exerted on charged particle are		Field lines	Tangent lines	Curved lines
6	Electric field lines are	Real	Imaginary	Perpendicular	Parallel
7	Electric field lines never –each other	Attract	Intersect	Repel	None
8	Electric lines are closer where the field	Weak	Strong	Negligible	Zero
9	Electric field lines due to a charge in	One D	Two-D	Three-D	Four-D
10	Closeness of field lines is the measure of	Direction of potential	Direction of field	Strength of field	Uniformity of field
11	A charge of 4 C is in the field of 4 N/C, the force on charge is	8N	<u>16N</u>	4 N	1 N
. 12	The force on an electron in a field of	2.6*10 <sup>-8</sup> N	2.88*10 <sup>-11</sup> N	2.6*10 <sup>-19</sup> N	1.6*10 <sup>-27</sup> N

1.8\*10<sup>8</sup> N/C

13 The unit of electric Newton Coulomb Joule/coulomb <u>Newton/coulomb</u> field intensity is

14 An electric field can Neutron Gamma <u>Beta particles</u> Gamma particle

deflect

15 If the magnitude of Doubled Halved Unaffected One fourth charge and distance are pakcity.org

both doubled then intensity of field

There are two applications of Electrostatics:

a) Xerography b) Inkjet printers

What is inkjet printer? Write principle and working.

Inkjet printer: "Such a printer which uses electric charge in its working is called inkjet printer".

Principle: Inkjet printers works on the principle of Electrostatics.

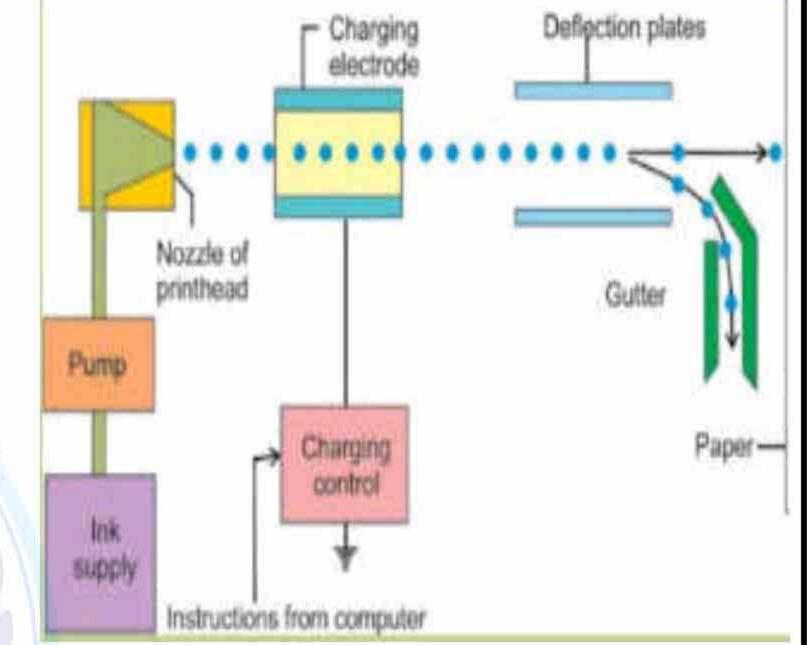
"It eject a thin stream of ink when shuttling back and forth across the paper and ink is ejected from small nozzle and break into small droplets".

#### Working:

An inkjet print head eject a steady flow.

Of ink droplets. The charging electrodes are used
To charge the droplet that are not need on the paper
Charged droplets are deflected into a gutter by the
Deflection plates, while uncharged droplets fly straight
Onto the paper.

Inkjet printer also produce colored images.



### Q. Write A Note On Xerography?

<u>Xerography (Photo copier):</u> It is Greek word, Xero mean dry; graphos mean writing, and Xerography mean dry writing. "The copying process is called Xerography".

toner cartridge

toner dust

paper on which the

image is printed

containing black

conductor

<u>Photocopier works on the following principle</u>: Photocopier works on the principle of Electrostatics.

"The lamp transfer image of page to the drum which leaves the static charge. The drum collects the toner dust and transfer it to the paper, the toner is melted on page".

### Main parts of photocopier: 1) Drum 2) toner 3) heated rollers

Drum is the heart of photocopier machine. Dum is an aluminum cylinder coated with layer of selenium.

Such materials which show conduction only when light falls on them, otherwise they are insulators in absence of light are called photoconductors like selenium.

**Working**: If the drum is exposed to an image of document to be copied, the dark and light areas of document produce same dark and light areas on the drum.

The dark areas retain their positive charge but light areas becomes conducting, in this way a positive charge image of document remains on the selenium surface, then a special dry black powder called "Toner" is given a negative charge and spread over the drum, where it sticks to the positive charge areas, the toner from the drum is transferred on to a sheet of paper on which document is to be copied, heated pressure rollers then melt the toner into the paper to produce permanent image of document.

### Multiple choice questions

heated rollers

printed image

drum

Electronics Electricity **Electrostatics** Photo copier and Magnetism inkjet printers are the applications of WC chamber One of the practical **Photo** Laser x-ray machine application of <u>copier</u> electrostatic induction is Aluminum Which one is photo Selenium Mercury Copper

4 word" Xerography " Writing by Writing be <u>Dry</u> Writing by means left hand children <u>writing</u> water colors

5 Photocopying process photography <u>Xerography</u> Scanning Holography

is called

6 In photocopier special Positive Neutral none black powder called charge toner gives Neutral none pakcity.org

### Q. DEFINE ELECTRIC FLUX. CALCULATE THE ELECTRIC FLUX THROUGH A SURFACE ENCLOSING A CHARGE

<u>Definition</u>: "Total number of electric field line passing normally through certain area is called electric flux.

OR: The scalar or dot product of electric field intensity and vector area is called electric flux"

Equation with unit:  $\varphi_e = \vec{E}.\vec{A}$ , =  $EA\cos\theta$  its unit is  $Nm^2C^{-1}$ ,

it is scalar quantity. is Greek letter. Electric flux depends on electric field intensity, vector area and orientation of surface.

Cases of electric flux: When angle b/w electric field and vector area  $=0^{\circ}$  =EAcos0°=EA= maximum electric flux

When angle b/w electric field and vector area =90°, =EAcos90°=0= minimum electric flux

<u>Vector area</u>: An area whose magnitude is equal to surface area A of the element but its direction is normal to this area is called vector area.

#### ELECTRIC FLUX THROUGH A SURFACE ENCLOSING A CHARGE

Consider a closed surface in the form of sphere of radius r having charge q. The surface is divided into n small patches of vector area are  $\Delta A_1$ ,  $\Delta A_2$ ,  $\Delta A_3$ .... $\Delta A_n$  so that each patch is a flat. Electric intensity for each patch are E<sub>1</sub>, E<sub>2</sub>, E<sub>3</sub>, E<sub>n</sub> respectively. pakcity.org

for first patch  $\varphi_{e1} = \vec{E}_1 . \Delta \vec{A}_1$ ,

for 2nd patch  $\varphi_{e_2} = \vec{E}_2 \cdot \Delta \vec{A}_2$ 

for 3rd patch  $\varphi_{e_3} = \vec{E}_3 . \Delta \vec{A}_3$ 

and so on...similarly

for nth patch  $\varphi_{e_n} = \vec{E}_n . \Delta \vec{A}_n$ 

Total electric flux through closed surface will be

$$\varphi_{\text{total}} = \varphi_1 + \varphi_2 + \varphi_3 + \dots \varphi_n$$
 putting values

$$\varphi_{\text{total}} = \vec{E}_1 \cdot \Delta \vec{A}_1 + \vec{E}_2 \cdot \Delta \vec{A}_2 + \vec{E}_3 \cdot \Delta \vec{A}_3 + \dots \vec{E}_n \cdot \Delta \vec{A}_n$$

$$\varphi_{\text{total}} = E_1 \Delta A_1 \cos \theta + E_2 \Delta A_2 \cos \theta + E_3 \Delta A_3 \cos \theta + \dots E_n \Delta A_n \cos \theta$$

As the direction of electric intensity and vector area is same at each patch so  $\theta = 0^{\circ}$ 

$$\varphi_{\text{total}} = E_1 \Delta A_1 \cos 0^{\circ} + E_2 \Delta A_2 \cos 0^{\circ} + E_3 \Delta A_3 \cos 0^{\circ} + \dots E_n \Delta A_n \cos 0^{\circ}$$
  $\cos 0^{\circ} = 1$ 

$$\varphi_{\text{total}} = E_1 \Delta A_1 + E_2 \Delta A_2 + E_3 \Delta A_3 + \dots = E_n \Delta A_n$$
 As we know that  $E_1 = E_2 = E_3 \dots = E_n = E$  for each patch

$$\varphi_{\text{total}} = E(\Delta A_1 + \Delta A_2 + \Delta A_3 + \dots \Delta A_n) = E(\text{Total Area of sphere})$$

As 
$$E = \frac{1}{4\pi\varepsilon_0} \frac{q}{r^2}$$
 surface Area of sphere  $= 4\pi r^2$ 

surface Area of sphere = 
$$4\pi$$
 r

$$\varphi_e = \frac{1}{4\pi\varepsilon_o} \frac{q}{r^2} (4\pi r^2) = \frac{q}{\varepsilon_o}$$

$$\varphi_e = \frac{q}{\varepsilon_o}$$
.....Req Result,



### State and prove Gauss's law?

Statement: Electric flux through any closed surface is equal to 1/ε<sub>ο</sub> times the total charge enclosed in it"

$$\varphi_e = \frac{1}{\varepsilon} * Q$$

Mathematically it can be written as

**Proof**: consider a closed surface having n point charges

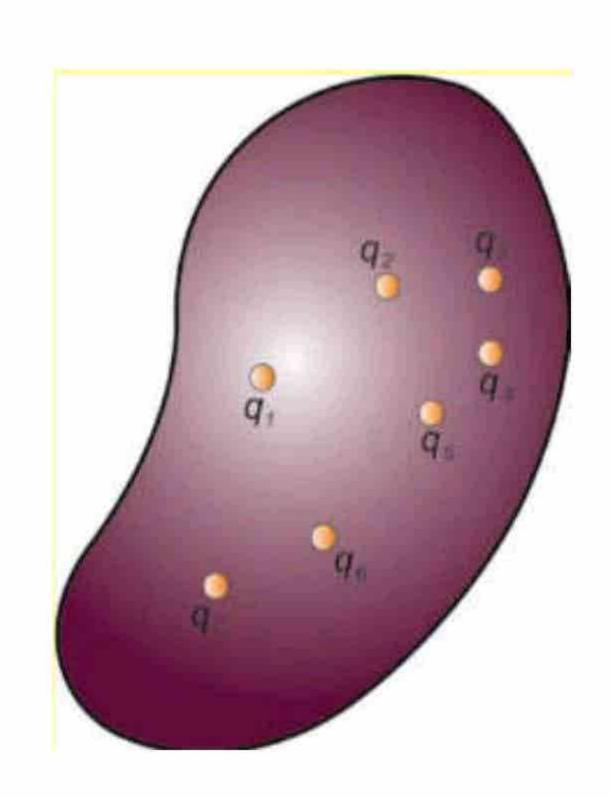
q<sub>1</sub>,q<sub>2</sub>,...on, total electric flux is calculated as

flux due to first point charge  $q_1 = \varphi_1 = \frac{q_1}{\varepsilon_o} - - - - - (1)$ 

flux due to 2nd point charge  $q_2 = \varphi_2 = \frac{q_2}{\varepsilon_o} - - - - - (2)$ 

flux due to 3rd point charge  $q_3 = \varphi_3 = \frac{q_3}{\varepsilon_o} - - - - - (3)$ 

flux due to nth point charge  $q_n = \varphi_n = \frac{q_n}{\varepsilon_o} - - - - - (n)$ 

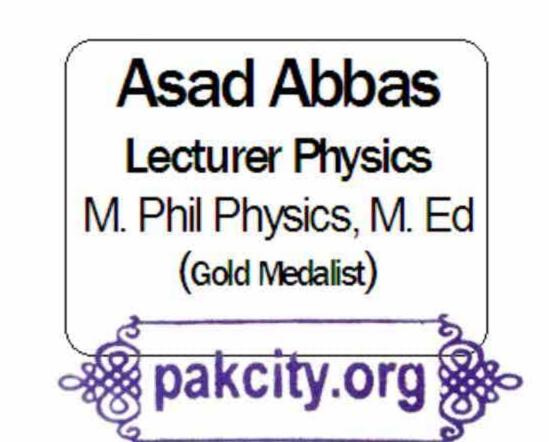


$$\varphi_{\text{total}} = \varphi_1 + \varphi_2 + \varphi_3 + \dots \varphi_n$$

$$\varphi_{\text{total}} = \frac{q_1}{\varepsilon_o} + \frac{q_2}{\varepsilon_o} + \frac{q_3}{\varepsilon_o} + \dots \frac{q_n}{\varepsilon_o}$$

$$\varphi_{\text{total}} = \frac{1}{\varepsilon_o} * (q_1 + q_2 + q_3 + \dots q_n)$$

$$\varphi_{\text{total}} = \frac{1}{\varepsilon_o} * (Total \text{ charge enclosed surface}) = \frac{1}{\varepsilon_o} * Q = \text{Req result}$$



### Applications of Gauss law

To calculate the electric field intensity we take following steps.

Step 01: Construct a Gaussian surface and charge enclosed by it.

Gaussian Surface: "An Imaginary closed surface which passes through point we want to calculate field is called Gaussian surface".

Step 02: Calculate the electric flux through the surface

Step 03: Calculate the electric field by applying Gauss's law.

Q. Calculate the Intensity of field inside a hollow charged sphere?

To calculate the field intensity inside a charged sphere.

Step 01: Construct a Gaussian surface of R'

inside the sphere in which there is no charge q=0

Step 02: To calculate the flux use formula  $\varphi_{\rm e}=\vec{\rm E}.\vec{\rm A}$  ----- (1

Step 03: Using Gauss's law  $\varphi_{total} = \frac{1}{\varepsilon_o} * q$  as there is no charge

in surface so flux is zero then

Equation 1)  $\varphi_e = \vec{E} \cdot \vec{A} = 0$  so this result into  $\vec{E} = 0$  inside the sphere.

Q.CALCULATE THE ELECTRIC INTENSITY DUE TO AN INFINITE SHEET OF

#### CHARGE.

Consider an infinite sheet on which positive charge is uniformly distributed.

To calculate the electric intensity at any point

® pakcity.org

**Step 01**: consider a Gaussian surface in the form of cylinder passing through sheet having Area A and  $\sigma$  is uniform **surface charge density**, so the charge enclosed by it is  $\mathbf{q} = \sigma \mathbf{A}$ 

Step 02: For calculation of electric flux through each surface of Gaussian cylinder

$$total\ flux = flux\ t\ roug\ rig\ t\ flat\ surface + flux\ t\ roug\ left\ flat\ + flux\ t\ roug\ curved\ surface$$

$$\varphi = \bar{E}.A + \bar{E}.A + no$$
 field lines passing t roug cuved surface

$$\varphi = EAcos\theta + EAcos\theta + 0$$
  
 $\Theta = 0^{\circ}$ 

as E and A are parallel so angle

 $\varphi e = EAcos0^{\circ} + EAcos0^{\circ} = EA + EA = 2EA -----(1)$ 

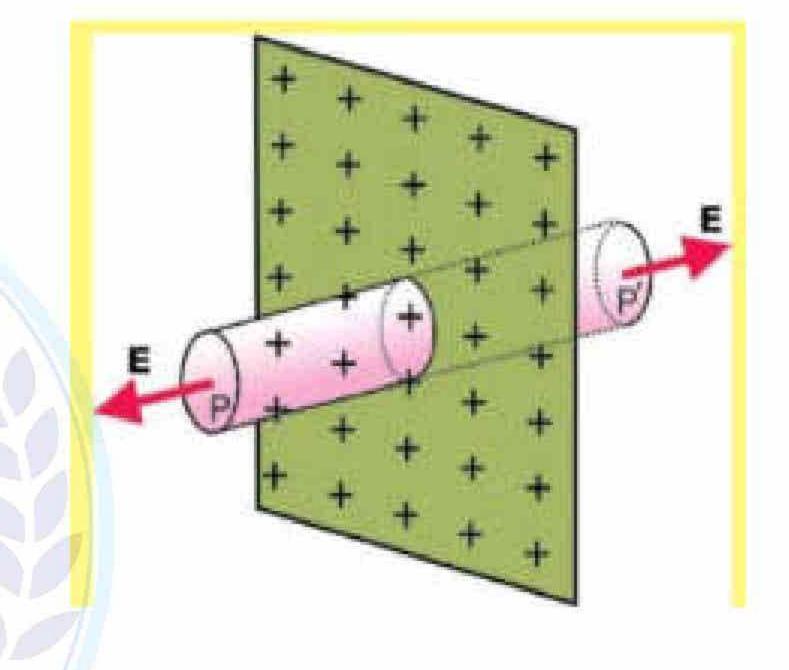
Step 03: According to Gauss's law  $\varphi_{total} = \varphi_{total} = \varphi_{tot$ 

Comparing both eqs.

2EA=
$$\frac{1}{\varepsilon_o}$$
\* q putting the value of q so

$$2EA = \frac{1}{\varepsilon_o} (\sigma A) \qquad E = \frac{\sigma}{2\varepsilon_o}$$

In vectorial form 
$$\vec{E} = \frac{\sigma}{2\varepsilon}$$



### Q. CALCULATE THE ELECTRIC INTENSITY B/W TWO OPPOSITELY CHARGED PARALLEL PLATES

Consider two parallel plate of closely spaced having opposite uniform distributed charge. Electric field lines start from positive plate and end on negative plate

**Step 01**: Consider a Gaussian surface in the form of hollow box having Area A and  $\sigma$  is uniform surface charge density, so the charge enclosed by it is  $q=\sigma A$ 

pakcity.or

Step 02: For Calculating electric flux through each surface of hollow box we follow

Total electric flux= flux through upper surface of box+ flux through lower surface of box+ flux through sides of box

As there is no field through upper end of box so flux through it will be zero

Flux through lower surface=  $\varphi = EAcos\theta = EAcos0^{\circ} = EA$ 

Flux through side of box is zero because they are parallel to field lines

So total electric flux becomes=  $\varphi_e$ =0+EA+0=EA -----(1)

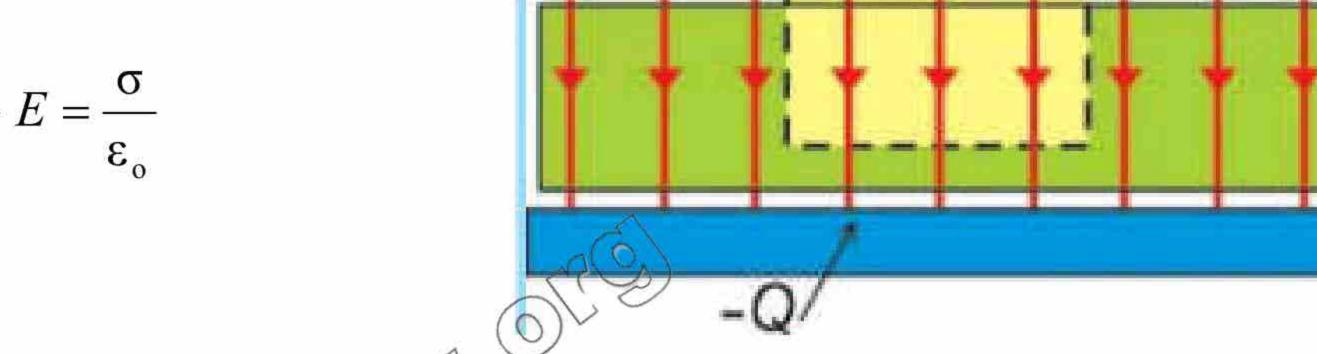
**Step 03**: According to Gauss's law  $\varphi_{total} = \frac{1}{2} * q$  ----(2)

comparing both equations to get the result

$$EA = \frac{1}{\varepsilon_o} * q \implies EA = \frac{1}{\varepsilon_o} * \sigma A \implies E = \frac{\sigma}{\varepsilon_o}$$

$$\Rightarrow E = \frac{\sigma}{\varepsilon_0}$$

in vectorial for  $\vec{E} = \frac{\sigma}{\hat{r}} \hat{r}$ 



### Multiple choice questions

For the computation of electric flux the surface should be

Closed Curved

Inclined Spherical

SI unit of electric flux IS

Nm<sup>2</sup>C<sup>-1</sup> NCm<sup>-2</sup>

 $\text{Nm}^{-2}\text{C}^{-3}$ 

Negative

3 When vector area L is held perpendicular to electric field lines then magnitude of electric flux is

Maximum Minimum

Either maximum or minimum

Electric flux depends 4 upon

Electric intensity

Area of surface

Orientation of area

All of these

5 Electric flux is a:

Vector, Nm<sup>2</sup>C<sup>-1</sup>

Scalar, Nm<sup>2</sup>C

Scalar ,Nm<sup>2</sup>C<sup>-1</sup> Vector,Nm<sup>2</sup>C<sup>-</sup>

What does Nm<sup>2</sup>C<sup>-1</sup> 6 stands for quantity

Electric field

Spherical

Electric potential

Cylindrical

**Electric** <u>flux</u>

Conical

Electric force

<u>Flat</u>

Equation Ø=**E.A** is applicable to surface

90°

<u>0°</u>

270°

180°

,					
	maximum electric flux is obtained when angle between $\overline{\pmb{E}}$ and $\overline{\pmb{A}}$ is				
9	Which one of the following can be taken as measure of electric field intensity	$rac{F}{A}$	$\frac{\phi_e}{A}$	$\frac{qA}{\varepsilon_o}$	$\frac{\varphi_e \varepsilon_o}{A}$ akcity.org
10	Electric field intensity inside a hollow charge sphere	$rac{oldsymbol{\sigma}}{oldsymbol{arepsilon}_o}$	$rac{\sigma}{2arepsilon_o}$	<u>Zero</u>	None
11	Electric field intensity due to infinite sheet of charge	$rac{\sigma}{\mathcal{E}_o}$	$rac{\sigma}{2arepsilon_o}$	Zero	None
12	Electric field intensity between two oppositely parallel plates	$rac{\sigma}{arepsilon_o}$	$\frac{\sigma}{2\varepsilon_{o}}$	Zero	None
13	Electric field due to infinite sheet isof between two oppositely parallel plates	Half Colon	Double	Four times	Same as
14	Surface charge density is equal to	Charge/area	Charge/field	Field/ charge	Force/ charge
15	SI unit of surface charge density	C/m <sup>2</sup>	C/m	Nm	N/C
16	Special organ called ampullae of lonrenzini that are sensitive to E	Bats	ty.oCats	Dogs	<u>Sharks</u>
17	Electric flux does not depend upon	Charge enclosed	Medium	Both A&B	Shape of closed surface
18	Statement $\varphi_{\rm e} = \frac{\rm Q}{\epsilon_{\rm o}}$ given by	Fermi	Coulomb	Farad	Gauss
					∎S :

19	Negative sign in electric potential gradient shows that electric intensity is along	Increasing potential	Increasing strength	<u>Decreasing</u> <u>potential</u>	Negative potential akcity.org
20	Gauss law is applied only to a surface which is	Open	Straight	<u>Closed</u>	All of these
21	A rubber ball of radius 2cm has charge 5C on its surface, E at its center is	10 N/C	2.5 N/C	Zero	5 N/C

What is Electric potential and potential difference? Write SI unit with formula.

Electric potential: "The electric potential energy per unit charge is called electric potential". V=W/q. Its unit is J/C which is equal to volt.

<u>Potential difference</u>: "The amount of work done in moving a charge from one point to other against electric field keeping the charge in equilibrium is called potential difference". OR

The difference of potential energy per unit charge b/w two points is called potential difference  $\Delta V = \frac{\Delta U}{a}$  and unit is volt.

Volt: SI unit of electric potential and potential difference is volt

<u>Definition of volt</u>: "If one joule of work is done in carrying a unit positive charge of 1 coulomb from one point to other keeping the charge in rest position, then potential difference will be one volt".

1 joule/Coulomb=1 volt

Q. What is Potential gradient? Derive its relation.

<u>Definition</u>: "The quantity  $\frac{-\Delta V}{\Delta x}$  gives the maximum rate of change of potential with respect to distance which is called the potential gradient". Its unit is V/m.

Relation: consider uniform Electric field E b/w two oppositely charged parallel plates and charge is moved again field pakcity.org

The potential difference b/w two points

$$V_{B} - V_{A} = \frac{W_{AB}}{q_{o}} = \frac{\vec{F}.\vec{d}}{q_{o}} = \frac{q_{o}Ed\cos\theta}{q_{o}} = \frac{q_{o}Ed\cos180^{o}}{q_{o}} = -Ed$$
  $\cos180^{o} = -1$ 

$$\cos 180^{\circ} = -1$$

as the distance b/w plates is small so  $d = \Delta r$  then above equation becomes

$$V_{\rm B} - V_{\rm A} = \Delta V = -E(\Delta r)$$

$$E = -\frac{\Delta V}{\Delta r}$$

Prove that 
$$\frac{1 \text{ newton}}{1 \text{ colomb}} = \frac{1 \text{ Volt}}{1 \text{ meter}}$$

as we know that 1volt= 1J/C, and joule= Nm

Required result

Q. What is absolute potential? Calculate the Electric potential due to a point charge.

<u>Definition</u>: "The work done in bringing a unit positive charge from infinity to that point keeping electrostatic equilibrium is called absolute potential pakcity.org or electric potential at a point".

Calculation of potential: Consider a positive point charge q is moved from infinity to that point keeping it in equilibrium, since electric field intensity changes inversely to square of distance, so it does not remains same so taken two points A and B close to each other so that E remains same

The distance of point A from charge  $q = r_{A}$ 

The distance of point B from charge  $q = r_B$ 

The mid point b/w A and B is given as  $r = \frac{r_A + r_B}{2}$ , and the magnitude of field at this point

since the points are close to each other so we take approximations

 $r_A \approx r_B = r$  so we can say that  $r^2 = rxr = r_A r_B$  so the field becomes

$$E = \frac{1}{4\pi\varepsilon_{o}} \frac{q}{r_{A}r_{B}}$$

now using the formula of potential gradient  $\Delta V = -E\Delta r$ 

$$V_B - V_A = -E(r_B - r_A)$$
 it may also written as

$$V_A - V_B = -E(r_A - r_B)$$
, applying minus inside the bracket  
 $V_A - V_B = E(r_B - r_A)$  putting the value of field

$$V_A - V_B = E(r_B - r_A)$$
 putting the value of field

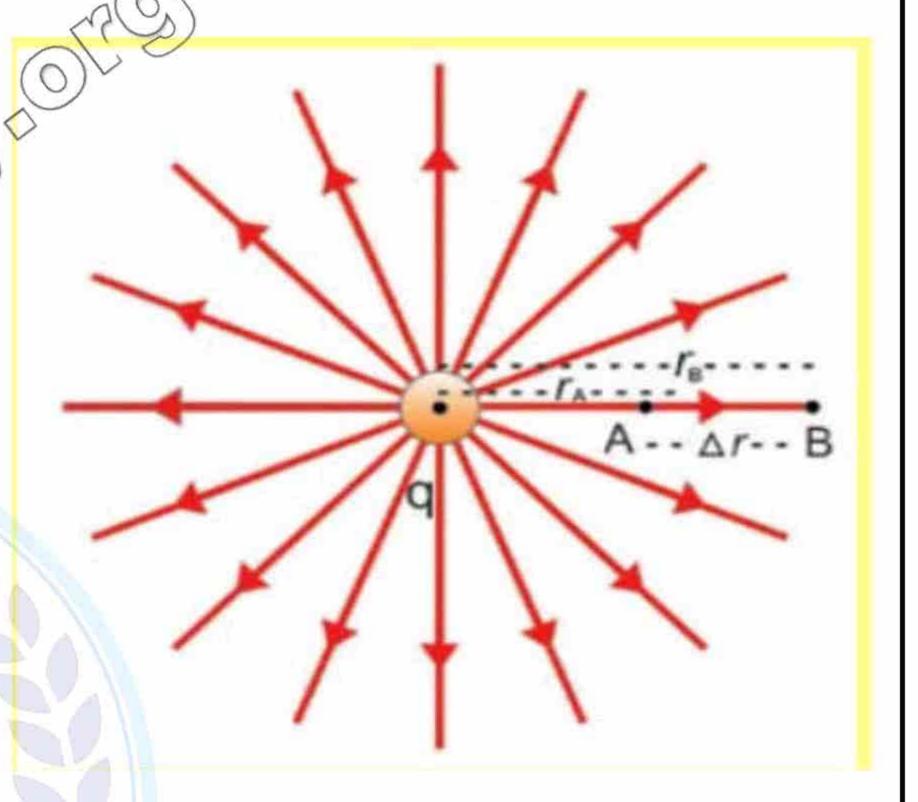
$$V_{A} - V_{B} = \frac{1}{4\pi\varepsilon_{o}} \frac{q}{r_{A}r_{B}} (r_{B} - r_{A}) = \frac{q}{4\pi\varepsilon_{o}} (r_{A}r_{B})$$

$$V_{A} - V_{B} = \frac{q}{4\pi\epsilon_{o}} (\frac{r_{B}}{r_{A}r_{B}} - \frac{r_{A}}{r_{A}r_{B}}) = \frac{q}{4\pi\epsilon_{o}} (\frac{1}{r_{A}} - \frac{1}{r_{B}})$$

As the point B is at infinity so  $r_B = \infty$  and  $V_B = 0$  and  $\frac{1}{1} = \frac{1}{1} = 0$ 

$$V_{A} - 0 = \frac{q}{4\pi\varepsilon_{o}} \left(\frac{1}{r_{A}} - 0\right) = \frac{q}{4\pi\varepsilon_{o}} \frac{1}{r_{A}}$$

in general V =  $\frac{q}{4\pi\varepsilon_0}\frac{1}{r}$ , this is electric potential due to a point charge.



What is eV? Prove that 1eV=1.6\*10<sup>-19</sup> J. and pakeity.org

Electron volt: "The amount of energy acquired or lost by an electron as it moves through a potential difference of one volt is called electron volt". This change in potential energy appears as kinetic energy q=e=1.6\*10<sup>-19</sup> C

$$\Delta(K.E)=q\Delta V$$

Electron Volt (eV) is the unit of energy

### Q. Write two similarities b/w electric force and gravitational force.

- 1) Both forces are conservative
- 2) Both obey inverse square law

### Q. Write four differences b/w electric and gravitational force.

**Electric force** 

**Gravitational force** 

Formula 
$$F = K \frac{q_1 q_2}{r^2}$$

Formula 
$$F = G \frac{m_1 m_2}{r^2}$$

It is explained by Coulomb law

It is stronger than gravitational force

It is explained by Gravitation law

It is weaker than electric force

It may be attractive or repulsive

It is medium dependent

It is attractive force only

It is medium independent

It is short range

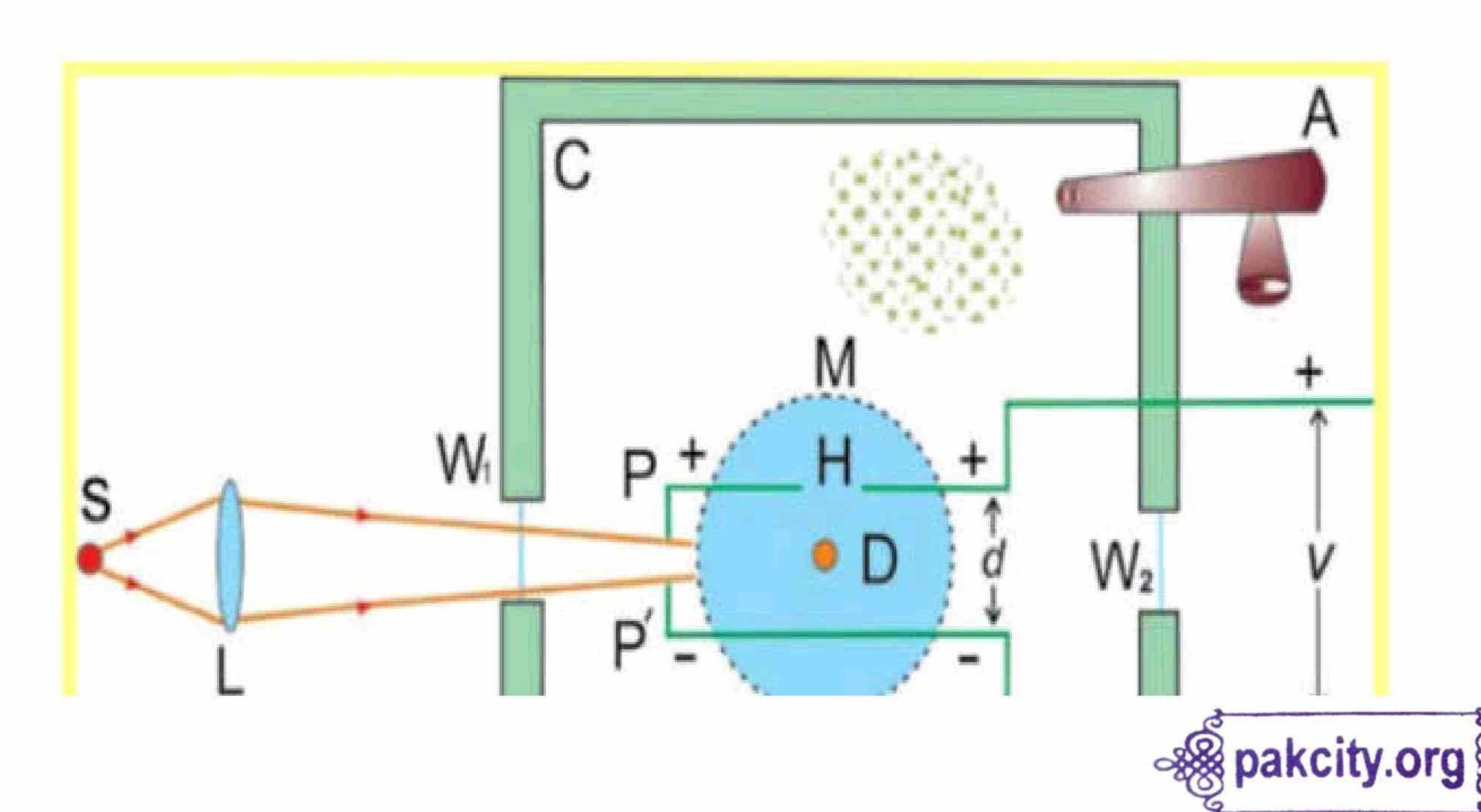
It is long range

### Q. DESCRIBE EXPERIMENT FOR FINDING THE CHARGE ON ELECTRON BY MILLIKAN OIL DROP METHOD.

<u>Definition</u>: "Such a technique which is used for finding the charge on electron devised by Millikan in 1909".

\*\*pakcity.org\*\*

<u>Construction</u>: The apparatus of this experiment consists of a evacuated chamber in which two parallel plates P and P' are placed at separation d, upper plate has small hole H. A potential difference is applied b/w plates to produce E. An atomizer is used for spraying oil drops into the chamber and light source S make the drops visible.



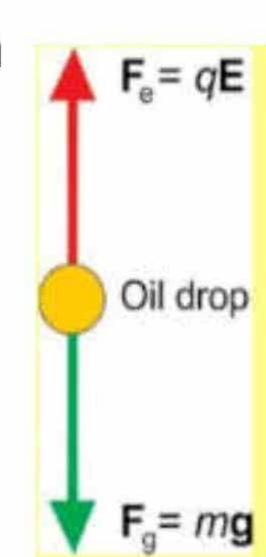
**Working**: The tiny oil droplets are sprayed into the chamber through small nozzle of atomizer which get charged negatively due to friction b/w walls of atomizer and oil drops. A potential difference is applied in such a way that electric force F=qE becomes equal to gravitational force(mg).

Charge on droplet: When electric force is equal to weight of droplet then

$$F_e = F_g$$
  $\Rightarrow$  also we know  $F_e = qE$ ,  $F_g = mg$ 
 $qE = mg$  also we know that  $E = \frac{V}{d}$ 

$$q\frac{V}{d} = mg$$

$$q = \frac{mgd}{V}$$
 which is the result for charge on droplet



Mass and radius of droplet: For calculation of mass of droplet the electric field is switched off so droplet falls under the action of gravity through air with terminal speed Vt. In this case weight must equal to drag force so

 $F = 6\pi\eta r v_t = mg - - - (1)$ , where r is radius of droplet, if  $\rho$  is density then  $\rho = m/v$ olume  $m = \rho * v$ olume  $= \rho * 4/3 \pi r^3$  putting the value in equation (1)  $6\pi\eta r v_t = \rho * 4/3 \pi r^3 g$ 

$$r^2 = \frac{18\eta v_t}{4\rho g} = \frac{9\eta v_t}{2\rho g}$$

$$r = \sqrt{\frac{9\eta v_t}{2\rho g}}$$
, this is the value of radius by knowing it we can find the mass of droplet

Conclusion: Millikan measured the charge on many droplets and found each droplet is the integral multiple of 1.6\*10<sup>-19</sup>C and concluded that the minimum value

of charge in nature is the charge on an electron

	$\underline{\mathbf{M}}$	ice Questions	a pakc	ity.org	
1	An ECG records, between points on human skin generated by electrical process in the heart	Current	<u>Voltage</u>	Resistance	Capacitano
2	The amount of energy equal to	One volt	One milli volt	One electron volt	One mega electron vc
	1.6x10 <sup>-19</sup> J is called				
3	1 volt is equal to	J <sup>-1</sup> C <sup>-1</sup>	<u>JC<sup>-1</sup></u>	J <sup>-1</sup> C	JC
4	Electron Volt is the unit of	Electricity	Voltage	Charge on electron	<u>Energy</u>
5	Electric potential at mid point in an electric dipole	<u>0 V</u>	50V	1V	1.5 V
6	Electrical energy is measured in	Watt	Horse power	Killo watt	<u>Killo watt</u> <u>hour</u>
7	A particle having charge 2e falls through a potential difference of 5V. energy acquired by it is	2.5eV	20eV	0.4eV	10eV
8	If an electron of charge is accelerated through a potential difference V, it will acquire energy	ve Maria Mar	V/2	E/2	Ve <sup>2</sup>
9	Potential gradient is defined as	<u>V</u>	$\frac{E}{r}$	$\frac{V}{E}$	None of these
10	A particle carrying a charge of 2e falls through a potential difference of 3V, energy acquired by it	9.6x10 <sup>-16</sup> J	9.6x10 <sup>-20</sup> J	9.6x10 <sup>-15</sup> J	9.6x10 <sup>-19</sup> J

is  $6.4x10^{-19}J$ 3.2x10<sup>-19</sup>J 1.6x10<sup>-19</sup>J Zero The amount of energy acquired or lost by an alpha particle as it moves through potential difference of 1V is  $9x10^{6} V$  $9x10^{7}V$ 9x10<sup>8</sup>V 9x10<sup>9</sup>V 12 Absolute potential difference due to point pakcity.org charge of 1C at a distance of 1m **6.25x10<sup>18</sup>eV** 6.25x10<sup>-18</sup>eV 1.6x10<sup>-19</sup>eV 9.1x10<sup>-31</sup>eV 1 joule is equal to A particle carrying a 3eV 1.5 eV 0.66eV <u>6eV</u> 14 charge of 2e falls through a potential difference of 3V, energy acquired by it 2V <u>0 V</u> 15 0.5V Two opposite point charge of same magnitude separated by distance 2d, electric potential mid way between them is 16 Heart Liver Brain Hands In Electroene Phalography the P.D by the electrical activity of --- are used pakcity.org for diagnose **Potential** The electrical activity Current Resistance Capacitance difference of retina of eye generate—used in electro ritino graphy 1 N/C=? V/C 18 1 mC <u>1V/m</u> C/N 19 SI unit of electric **Volt** Farad Colomb joule potential and potential difference are

					<b>●</b> ○ <b></b>
20	SI unit of potential gradient is same as that of	Electric potential	Electric field intensity	Capacitance	None
21	1 joule/colomb is equal to	Farad	<u>Volt</u>	joule	Newton
22	If 5J of work done of an object having charge 5C than what will be potential	2 V	1 Volt	4 volt	25 Volt city.org
23	Which is the property of electric force	Obey inverse square law	Conservative force	Short range than gravity	All of these
24	Charge on electron determined by Millikan in	1906	1907	1908	<u>1909</u>
25	Millikan and Fleter could find the charge on oil droplets in	Thermal equilibrium	Electrical equilibrium	Mechanical equilibrium	Unstable equilibrium
26	The name electron was suggested by	Thomson	Rutherford	Millikan	<u>Stoney</u>
27	The electrical activity of retina of eye generate—used in electro ritino graphy	Current	Potential difference	Resistance	Capacitance
28	minimum value of charge in nature is the charge on	Electron	Alpha particle	Neutron	Muon
29	The minimum charge on an object in nature cannot be less than	ZeroCity	1.6x10 <sup>-19</sup> C	-1.6x10 <sup>-19</sup> C	±1.6x10 <sup>-19</sup> C
30	The unit of electric field intensity other than N/C is	V/A	<u>V/m</u>	V/C	N/V
31	$-\frac{\Delta V}{\Delta r}$ is called	Electric field	<u>Potential</u> gradient	Electric potential	Capacitance
32	SI unit of electric	Kgm <sup>2</sup> s <sup>-1</sup> /C	Kgm <sup>2</sup> s <sup>-2</sup> /C	Kgm <sup>2</sup> /C	Kgms <sup>-2</sup> /C

	potential is				
33	The charge on oil droplet in Millikan oil drop experiment is calculated using	q=mg/V	mgd/V	v/mgd  www.pakci	d/mgV ty.org
34	A charged conductor has charge on	<u>Outer</u> surface	Inner surface	Middle surface	None
35	If a charge is moved against electric field, will gain	Electric potential energy	Kinetic energy	Both A&B	None
36	Strength of field in order to suspend a charge q and mass m	E=mg/q	E=m/q	E=q/mg	Both A&B
37	In Millikan experiment, if the direction field is reversed then acceleration of particle	<b>2g</b>	g RETURNED	g/2	<b>4</b> g

### Q. WHAT IS CAPACITOR? CALCULAT THE CAPACITANCE OF PARALLEL PLATE CAPACITOR.

<u>Definition:</u> "A Device which is used to store charge as well as electrical energy is called capacitor".

<u>Construction</u>: A capacitor consists of two parallel plates having opposite charge connected to potential difference V. let the Q charge on either of plate. So  $Q \propto V \implies Q = CV$ , C is constant of proportionality called capacitance of capacitance

<u>Capacitance</u>: The ability of capacitor to store charge is called capacitance. C=Q/V, its unit is farad.

<u>Farad</u>: If a charge of one coulomb given to plates of capacitor produces a potential difference of one volt b/w them then capacitance is 1 farad. **1 Farad= 1C/1V**.

<u>Capacitance of parallel plate capacitor</u>: Let us consider a parallel plate capacitor consisting of two metal plates each of area A separated by small distance d as shown in fig

### Case A: When medium is air or vacuum b/w plates

If Q is the charge on the capacitor and V is the potential difference then

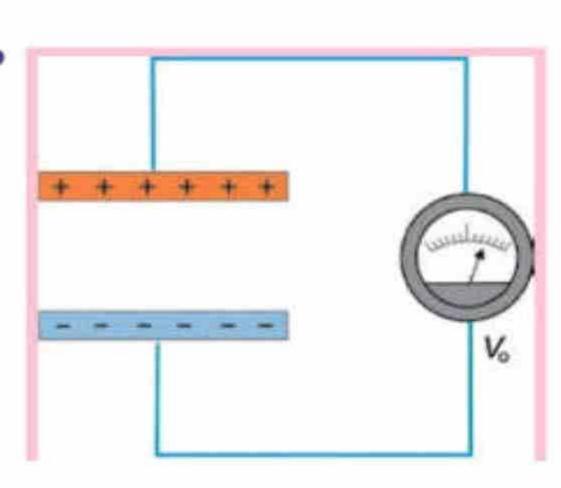
 $C_{vac} = \frac{Q}{V}$  --- (1) , the magnitude of electric intensity E is related with distance and potential

 $E = \frac{V}{I}$ , V = Ed also we know that Electric field intensity b/w two oppositely plates is  $E = \frac{\sigma}{\varepsilon_0}$ 

$$V = \frac{\sigma}{\varepsilon_o} d$$
 also we know  $\sigma = \frac{Q}{A}$  also we know  $\sigma = \frac{Q}{A}$ 

 $Q = \sigma A$ putting these values in eq (1)





$$C_{\text{vac}} = \frac{\sigma A}{\frac{\sigma}{\varepsilon_o} d}$$

 $C_{\text{vac}} = \frac{A\varepsilon_o}{A}$  this is the capacitance of parallel plate capacitor when air is placed b/w plates

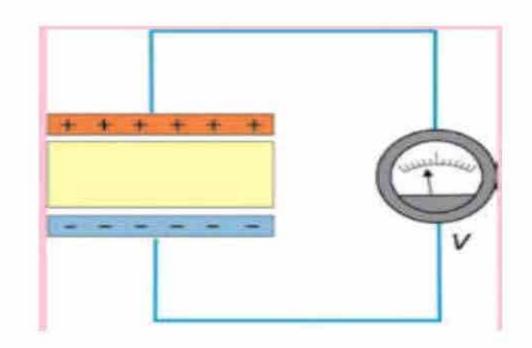
case B: If insulating medium called dielectric of relative permittivity  $\varepsilon_r$  is placed b/w plates then capacitance is increased by the factor  $\varepsilon_{\rm r}$  and the formula for this is  $C_{\rm med} = \frac{A\varepsilon_o \varepsilon_{\rm r}}{J}$ 

Dielectric constant: "The ratio of capacitance of parallel plate capacitor with dielectric as medium to its capacitance when air as medium b/w plates is called dielectric constant.

Its formula is  $\varepsilon_r = \frac{C_{med}}{C_{med}}$  having no unit.

$$\frac{C_{med}}{C_{vac}} = \frac{\frac{A\varepsilon_o \varepsilon_r}{d}}{\frac{A\varepsilon_o}{d}} = \varepsilon_1$$





Q.What is ELECTRIC POLARIZATION OF DIELECTRIC and also define electric dipole.

Electric Dipole: "Two equal and opposite charges placed at small distance d formed an electric dipole".

Polarization and polarized: "A process in which the molecules of the dielectric under the action of external electric field become dipoles is called electric polarization" and dielectric is called polarized.

OR "The phenomenon in which negative and positive charges of atoms/molecules of dielectric are slightly displaced when a dielectric is placed in an electric field is called polarization".

### Q. What is the effect of polarization on capacitance of capacitor?

**Ans**: When the dielectric is placed b/w plates then capacitance of capacitor is increased. Because dielectric material decrease surface charge density on plates which decrease electric field intensity  $E = \frac{\sigma}{\varepsilon_o}$ , with this potential difference V is decreased V=Ed and capacitance is increased C=Q/V.

### Q. CALCULATE THE ENERGY STORED IN CAPACITOR IN TERMS OF ELECTRIC FIELD.

Capacitor is device which is used for storing charge as well as electric energy".

When a capacitor is uncharged, the potential difference

b/w plates is zero and finally it becomes V when charge

is deposited on each plate.

Average potential = 
$$\frac{0+V}{2} = \frac{V}{2}$$

electric potential energy = Average potential x charge

P.E = 
$$\frac{V}{2}q$$
 Also we know that  $q = CV$ 

Energy stored in an electric field

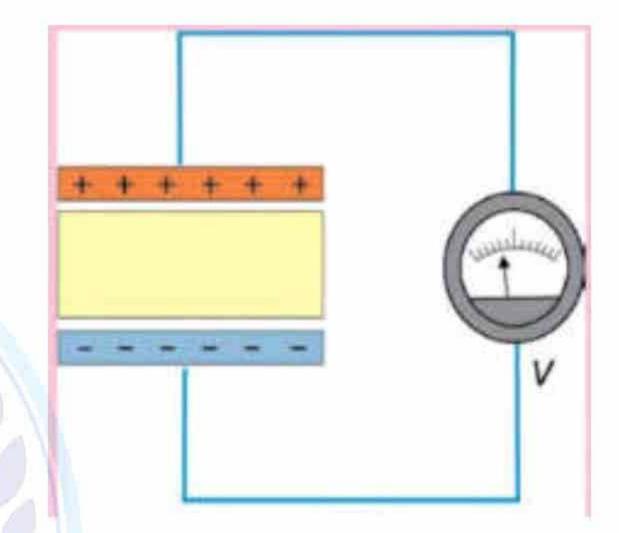
As we know that capacitance of capacitance C when medium is placed  $C = \frac{A\varepsilon_o \varepsilon_r}{d}$ , V = Ed

Energy = 
$$\frac{1}{2} \frac{A \varepsilon_o \varepsilon_r}{d} (Ed)^2 = \frac{1}{2} (E^2 \varepsilon_o \varepsilon_r) (Ad)$$

pakcity.org

. Energy = 
$$\frac{1}{2}$$
(E<sup>2</sup> $\varepsilon_o \varepsilon_r$ )(volume)

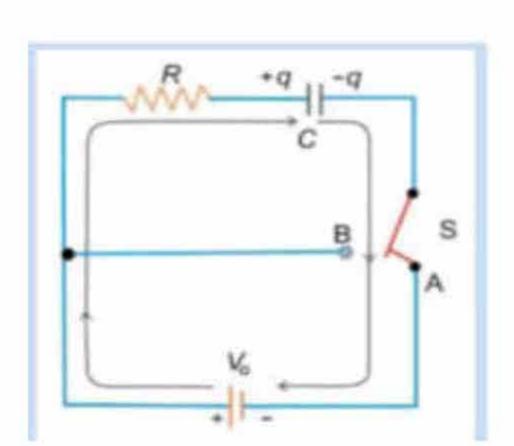
Energy/Volume = Energy density = 
$$\frac{1}{2}E^2\varepsilon_o \varepsilon_r$$
, This is required result

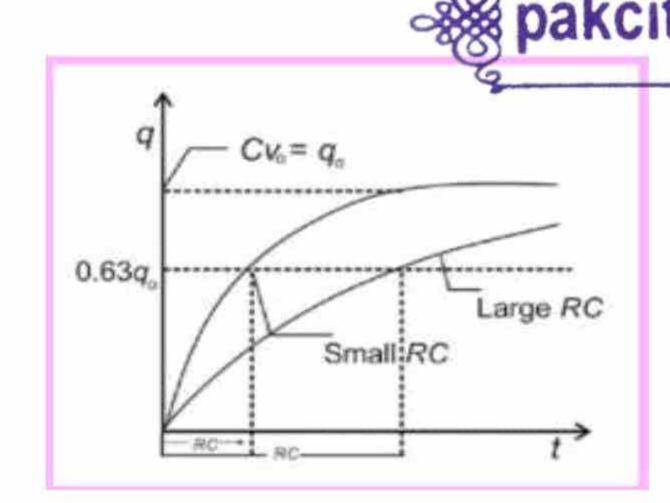


#### Q. DISCUSS CHARGING AND DISCHARGING OF CAPACITOR

**RC** circuit: The circuit consists of capacitor of capacitance C and resistor of resistance R is called RC circuit.

Charging of capacitor: When the switch S is set at terminal A connected to battery V which starts charging the capacitor through R. capacitor is not charged immediately and charges take some time to attain maximum value on capacitor qo=CVo

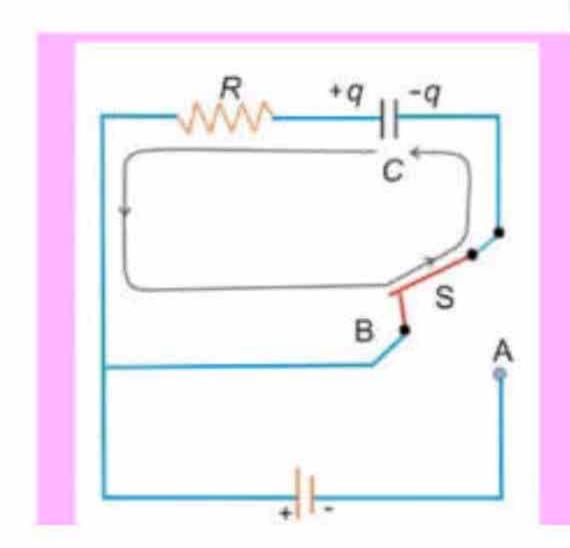


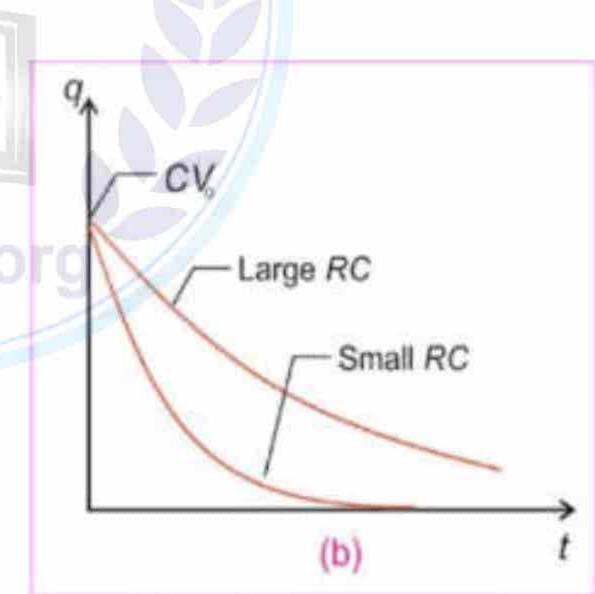


<u>Time constant</u>: "The time required by capacitor to charge 63% of its maximum value is called time constant". OR "the product of resistance and capacitance is called time constant t=RC". Its unit is second.

For small value of time constant capacitor rapidly/fastly charge and discharge.

<u>Discharging of capacitor</u>: When switch is set at a point B, charge on positive plate start to discharge through R and neutralize the negative plate and graph of discharging is shown in fig





Graph of charging and discharging of capacitor is exponential

### USEFUL INFORMATION AND TIDEBITS



✓ Write the principle of working of windshield wipers of cars?

Charging and discharging of capacitor enable windshield wipers to be used. The time of the on-off cycle is found by the time constant of resistor capacitor combination.

✓ If a surface encloses a positive as well as negative charge of same value. Then what is the value net flux?

The net value of flux will be zero

✓ Why electronic circuits such as T.V and computer are often enclosed within metal boxes?

To eliminate stray electric field interference circuits of such devices are enclosed within metal boxes.

pakcity.org

✓ What is ECG?

ECG stands for electro cardio gram. An ECG records the voltage b/w points on human skin generated by electrical process in the heart.

✓ What is EEG?

EEG stands for electro enephalo graph, in this potential difference created by the electrical activity of brain are used for diagnosing abnormal behavior.

✓ What is ERG?

ERG stands for Electro retino graphy, in which electrical activity of the retina of

eye generates the potential difference.

#### ✓ How shark and other sea creatures locate their prey very precisely?

Fish and other sea creatures produces electric field in variety of ways, sharks have special organ called ampullae of lorezini that are sensitive to field and can detect potential difference of **nanovolt** and can locate their prey very precisely

Pou	ential difference of <b>flamovoit</b> and	i Carriocat <del>e</del> ti	ieli piey vei		
	Multiple	choice que	estions	a pako	ity.org
1	Wind shield wipers of car to be used	Charging/ Dischargi ng	Potential effect	Compton effect	Ohm law
2	A 5Mega ohm resistor is connected with 2 micro farad capacitor. Time constant	0.1 sec	1 sec	2.5 sec	<u>10 sec</u>
3	Net charge on a capacitor is	Infinity	q	2q	<u><b>0</b></u>
4	The energy stored in capacitor is given by the relation	$\frac{1}{2}\varepsilon_{o}\varepsilon_{r}E^{2}$	$\frac{1}{2} \mathcal{E}_r E^2(Ad)$	$\frac{1}{2}\varepsilon_o\varepsilon_r E^2(A)$	$\frac{1}{2}\varepsilon_r E^2$
5	The product of resistance and capacitance is called	Force	<u>Time</u> <u>Constant</u>	Velocity	Current constant
6	The capacitance of a parallel plate capacitor is given by C=?	$A \in 0$ $\overline{d}$	$\frac{A \in 0}{q}$	$\frac{q \in 0}{d}$	None of these
7	If time constant in RC circuit is small, then capacitor is charged or discharged	Rapidly	Slowly	At constant rate	Nil
8	A charge of 10 <sup>-10</sup> C b/w two parallel plates 1cm apart experience a force of 10 <sup>-5</sup> N, the P.D is	Amber 10mg	100V	<u>1000V</u>	<b>1V</b>
9	Farad is defined as	C/V	A/V	C/J	J/C
10	The expression of energy stored in a capacitor is given by	E=cV <sup>2</sup>	E=1/2 CV <sup>2</sup>	E=1/2 C <sup>2</sup> V	E=1/2(CV) <sup>2</sup>
11	In capacitor, energy is stored in the	Magnetic field	<u>Electric</u> <u>field</u>	Gravitatio nal field	Nuclear field
12	In the time constant of RC circuit, how much charge is	0.37qo	0.51qo	<u>0.63qo</u>	0.90qo

	stored out of maximum charge qo				
13	Energy density in case of capacitor is always proportional to	<b>E</b> <sup>2</sup>	$\epsilon_{o}$	V <sup>2</sup> Residence of the second	city.org
14	The increase in capacitance of a capacitor due to presence of dielectric is due to of dielectric	Electric polarizatio n	Electrifica	Ionization	Electrolys
15	Energy stored per unit volume inside capacitor is called	Electric intensity	Electric flux	Energy density	Electrical energy
16	The unit of RC is	Volt	<u>Second</u>	Coulomb	Ampere
17	Product of resistance and capacitance is called	Gas constant	Resistivit	Boltzman n constant	<u>Time</u> constant
18	Farad is the unit of	Charge	Current	Electric flux	<u>Capacita</u> <u>nce</u>
19	A capacitor is perfect insulator for	AC AC	DC	Both A&B	None
20	Sec/ohm is equal to	Farad	Coulomb	Joule	Ampere
21	If potential difference between plates of parallel plate capacitor is doubled then energy stored in it will	Two times	Eight times	Four times	Remains same
22	SI unit of energy density of electric field is	J/C	J/V	<u>J/m</u> <sup>3</sup>	J/F <sup>3</sup>
23	The term "RC" has same unit as that of	Potential	Capacita nce	Energy	<u>Time</u>
24	A parallel plate capacitor with oil between plates dielectric constant=2 has capacitance C. if the oil removed than capacitance becomes		C/√2	2C	<u>C/2</u>
25	The capacitor stores energy in the form of	Magnetic field	Heat energy	Mechanic al energy	Electrical energy

26 If the dielectric is inserted Does not increase Becomes Decrease between the plates of a change zero

capacitor, the potential difference

27 Which material is used to Tin Mica Iron copper increase the capacitance of



1. The potential is constant throughout a given region of space. Is the electric field zero or non-zero in this region? Explain

Electric field will be zero in this region

We know that  $E = \frac{-\Delta V}{2}$ for constant potential  $\Delta V=0$ Then E=0

2. Suppose that you follow an electric field line due to a positive point charge. Do electric field and the potential increases or decreases?

Both electric field and potential will decrease as we know that  $E \propto \frac{1}{\pi^2}$  and  $V \propto \frac{1}{\pi}$ when we move away r increase and E and V will be decreased.

- 3. How can you identify that which plate of capacitor is positively charged? To identify the plate of a capacitor a gold leaf electroscope is used If the positive charged disc of gold leaf electroscope is touched with any plate of the charged capacitor and the divergence of the leaves increases, the plate of capacitor is positively charged (due to repulsion of similar charged plates). If the divergence of leaves decreases, then that plate of capacitor is negatively charged (due to force of attraction b/w different charged plates).
- 4. Describe the force or forces on a positive point charge when placed between parallel plates', with similar and equal charges ii. With opposite and equal charges?
  - Net force acting on the positive charge is zero as electric field intensity due to equal and opposite plate is zero so F=qE=0
  - Net force acting on the positive charge will be maximum due to maximum value of field in this case F=qE
- 5. Electric lines of force never cross. Why?

Electric lines of force never cross each other. This is because of the reason that electric field intensity has only one direction at any given pint. If the lines cross, electric intensity could have more than one direction which is physically impossible.

6. If a point charge of mass m is released in a non-uniform electric field with field lines in the same direction pointing, will it make a rectilinear motion?

Yes, it will make a rectilinear motion, If a point charge q of mass m is placed at any point in the field, it will follow straight or rectilinear path along the field line due to repulsive force.

## 7. Is E necessarily zero inside a charged rubber balloon if the balloon is spherical?

Yes, E is necessarily zero inside a charged rubber balloon. Because there is no charge enclosed by it so electric field will be zero.

$$\varphi_{\rm e} = \frac{\rm q}{\varepsilon_{\rm o}} = \frac{0}{\varepsilon_{\rm o}} = 0$$



$$\varphi_e = EA$$
, so  $EA = 0$  then  $E = 0$  as  $A \neq 0$ 

# 8. Is it true that Gauss's law states that the total number of lines of force crossing any closed surface in the outward direction is proportional to the net positive charge enclosed within surface?

Yes it is true statement, as Gauss's law states that number of electric field lines through any closed surface is 1/εο times the total charge enclosed in it as flux is directly proportional to charge so this statement is true.

9. Do electrons tend to go to region of high potential or of low potential? The electrons being negatively charge particle when released in electric field moves from a region of lower potential (negative end) to a region of high potential (positive end).

### CHAPTER = 12 NUMERICALS

12.1: Compare magnitudes of electrical and gravitational forces exerted on an object (mass = 10.0g, charge = 20.0 $\mu$ C) by an identical object that is placed 10.0cm from the first.  $(G = 6.67 \times 10^{-11} Nm^2 kg^2)$ 

Given Data: Mass  $m_1 = m_2 = m = 10g = 10/1000 \text{ kg} = 0.1 \text{ kg}$ , Charge  $q_1 = q_2 = 20 \mu\text{C} = 20 * 10^{-6} \text{C}$ , r = 10 cm = 10/100 = 0.1 m

solution: 
$$\frac{F_{e}}{F_{G}} = ? \Rightarrow \frac{F_{e}}{F_{G}} = \frac{Kq_{1}q_{2}}{Gm_{1}m_{2}/r^{2}} = \frac{Kqq}{Gmm_{2}} = \frac{9*10^{9}(20*10^{-6})^{2}}{6.67*10^{-11}(0.1)^{2}} = 5.4*10^{14}$$

12.3: A point charge  $q = -8.0 \times 10^{-8} \, C$  is placed at the origin. Calculate electric field at a point 2.0m from the origin on the z-axis.

Given Data: Charge =  $1 = -8 * 10^{-8} \text{ C}$ , r = 2 m, E = ?

solution: 
$$E = \frac{Kq}{r^2} = \frac{9*10^9*(-8*10^{-8})}{(2)^2} = -(1.8*10^2 \,\hat{K})N/C$$
,  $\vec{E}$  is along negative Z - axis

12.4: Determine the electric field at the position  $r = (4\hat{i} + 3\hat{j})m$  caused by a point charge  $q = 5.0 \times 10^{-6} \, C$  placed at origin.

Given Data : 
$$r = (4\hat{i} + 3\hat{j})m$$
,  $q = 5*10^{-6}$  C,  $E = ?\hat{r} = \frac{\vec{r}}{|\vec{r}|} = \frac{(4\hat{i} + 3\hat{j})}{\sqrt{4^2 + 3^2}} = \frac{(4\hat{i} + 3\hat{j})}{\sqrt{16 + 9}} = \frac{(4\hat{i} + 3\hat{j})}{5}$ 

Solution : As E = 
$$\frac{Kq}{r^2}\hat{r} = \frac{9*10^9*5*10^{-6}}{5^2} * \frac{(4\hat{i}+3\hat{j})}{5} = 360*(4\hat{i}+3\hat{j}) = (1440\hat{i}+1080\hat{j}) \text{ N/C}$$

12.5: Two point charges,  $q_1 = -1.0 \times 10^{-6} C$  and  $q_2 = +4.0 \times 10^{-6} C$ , are separated by a distance of 3.0m. Find and justify the zero-field location.

Given Data :  $q_1 = -1*10^{-6}$  C,  $q_2 = 4*10^{-6}$  C, r = 3m, Location at which  $\vec{E} = 0 = ?$  solution : consider P be a point at a distance x from charge  $q_1$  at which E is zero

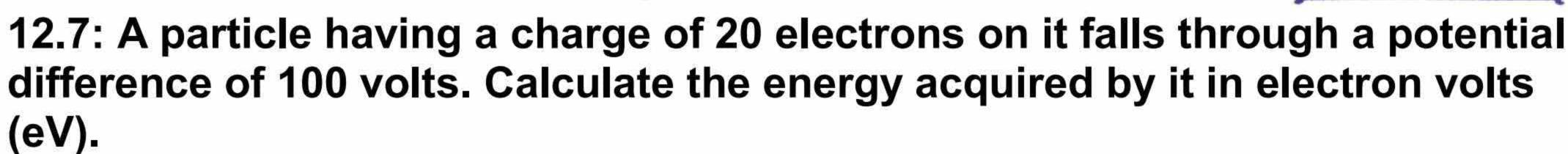
$$E_1 = \frac{Kq_1}{x^2}, \quad E_2 = \frac{Kq_2}{(x+3)^2}$$
 As  $E_1 = E_2 \Rightarrow \frac{Kq_1}{x^2} = \frac{Kq_2}{(x+3)^2} \Rightarrow \frac{q_1}{x^2} = \frac{q_2}{(x+3)^2}$ 

$$\frac{1*10^{-6} \,\mathrm{C}}{\mathrm{x}^2} = \frac{4*10^{-6} \,\mathrm{C}}{(\mathrm{x}+3)^2} \Rightarrow \frac{1}{\mathrm{x}^2} = \frac{4}{(\mathrm{x}+3)^2} \Rightarrow (\mathrm{x}+3)^2 = 4\mathrm{x}^2 \Rightarrow \mathrm{x}+3 = 2\mathrm{x} \Rightarrow \mathrm{x}=3\mathrm{m}$$

12.6: Find the electric field strength required to hold suspended a particle of mass and  $1.0 \times 10^{-6} kg$  charge  $1.0 \mu c$  between two plates 10.0cm apart.

Given Data: mass =  $m = 1*10^{-6}$  kg,  $q = 1\mu\mu = 1*10^{-6}$  C, d = 10cm = 10/100 m = 0.1 m,  $\vec{E} = ?$ 

solution: As 
$$\vec{F}_e = \vec{F}_g \Rightarrow q\vec{E} = mg \Rightarrow \vec{E} = \frac{mg}{a} = \frac{1*10^{-6}*9.8}{1*10^{-6}} = 9.8 \text{N/C} \text{ or } 9.8 \text{V/m} \approx 80 \text{ pakcity.org}$$



Given data: Nof electrons = n = 20, charge on electron =  $1.6*10^{-19}$  C,  $q = ne = 20*1.6*10^{-19}$  C

 $q = 3.2 * 10^{-18} C$ , potential difference =  $\Delta V = 100 V$ ,  $\Delta(K.E) = ?$ 

$$\Delta(K.E) = q\Delta V = 3.2*10^{-18} \text{ C}*100\text{V} = 3.2*10^{-16} \text{ J} \Rightarrow \text{ or } \Delta(K.E) = \frac{3.2*10^{-16}}{4.6*10^{-19}} \text{ eV} = 2*10^{3} \text{ eV}$$

- 12.8: In Millikan's experiment, oil droplets are introduced into the space between two flat horizontal plates, 5.00 mm apart. The plate voltage is adjusted to exactly 780V so that the droplet is held stationary. The plate voltage is switched off and the selected droplet is observed to fall a measured distance of 1.50 mm in 11.2s. Given that the density of the oil used is 900kgm
- <sup>3</sup>, and the viscosity of air at laboratory temperature is  $1.80 \times 10^{-5} Nm^{-2}s$ , calculate...(a) The mass, and (b) The charge on the droplet (Assume g =  $9.8 \text{ms}^{-2}$ )

Given Data :  $d = 5 \text{ mm} = 5*10^{-3} \text{ m}$ , V = 780 V,  $S = 1.55*10^{-3} \text{ m}$ , t = 11.2 sec,  $\eta = 1.8*10^{-5} \text{ Nm}^{-2} \text{S}$ ,  $\rho = 900 \text{kgm}^{-3}$ 

m=? q=? As we know that  $\rho=mass/Volume, \Rightarrow m=\rho*volume=\rho*4/3 \pi r^3----(1)$ 

As 
$$v = s/t = 1.55*10^{-3}/11.2 = 0.13*10^{-3} \text{ ms}^{-1}$$
,  $r = \sqrt{\frac{9\eta\eta}{2\rho\rho}} = \sqrt{\frac{9(1.8*10^{-5})0.13*10^{-3}}{2*900*9.8}} = 0.011*10^{-4} \text{ m, putting in (1)}$ 

 $m = \rho * 4/3 \pi r^3 = 900 * 4/3 * 3.14 * (0.011 * 10^{-4})^3 = 5.01 * 10^{-15} kg$ 

charge = 
$$q = \frac{mgd}{V} = \frac{5.01*10^{-15}*9.8*5*10^{-3}}{780} = 3.15*10^{-19}C$$

- 12.9: A proton placed in a uniform electric field of 5000 NC<sup>-1</sup> directed to right is allowed to go a distance of 10.0cm from A to B. Calculate.
  - (a) Potential difference between the two points
  - (b) Work done by the field
  - (c) The change in P.E. of proton
  - (d) The change in K.E. of the proton
  - (e) Its velocity (mass of proton is  $1.67 \times 10^{-27} kg$ )

Given Data :  $q = 1.6 * 10^{-19} \text{ C}$ ,  $m = 1.67 * 10^{-27} \text{ Kg}$ , E = 5000 N/C, d = 0.1 m,

(a) 
$$V = ? V = -Ed = -5000 * 0.1 = -500 V$$

(a) 
$$V = ?V = -Ed = -5000 * 0.1 = -500 V$$
 (b)  $W = ?W = qV = 1.6 * 10^{-19} C * 500 V = -500 eV$ 

(c) 
$$\Delta U = ?\Delta U = qV = 1.6*10^{-19} C*(-500 V) = -500 eV$$
, (d)  $\Delta K.E = ?\Delta K.E = qV = 1.6*10^{-19} C*500 V = 500 eV$ 

(e) 
$$v = ? \Delta K.E = \frac{1}{2}mv^2 \Rightarrow v = \sqrt{\frac{2\Delta K.E}{m}} = \sqrt{\frac{21.6*10^{-19}C*500 V}{1.67*10^{-27}}} = 3.09*10^5 m/s$$
 

(e)  $v = ? \Delta K.E = \frac{1}{2}mv^2 \Rightarrow v = \sqrt{\frac{2\Delta K.E}{m}} = \sqrt{\frac{21.6*10^{-19}C*500 V}{1.67*10^{-27}}} = 3.09*10^5 m/s$ 

12.10: Using zero reference point at infinity, determine the amount by which a point charge of  $4.0 \times 10^{-8} C$  alters the electric potential at a point 1.2m away, when (a) Charge is positive (b) Charge is negative.

Given Data :  $q = 4 * 10^{-8} C$ , r = 1.2 m, V + = ? V - = ?

$$V + = \frac{K(+q)}{r} = \frac{9*10^9(4*10^{-8})}{1.2} = +300V, V - = \frac{K(-q)}{r} = \frac{9*10^9(-4*10^{-8})}{1.2} = -300V$$

12.11 In Bohr's atomic model of hydrogen atom, the electron is in an orbit nuclear proton at a distance of  $5.29 \times 10^{-11} m$  with a around the speed of  $2.18 \times 10^6 \, ms^{-1}$ .

$$(e = 1.60 \times 10^{-19} C, mass of electron = 9.10 \times 10^{-31} kg)$$
. Find

- (a) The electric potential that a proton exerts this distance
- (b) Total energy of the atom in eV
- (c) The ionization energy for the atom in eV

Given Data :  $r = 5.29 * 10^{-11}$  m,  $v = 2.18 * 10^6$  m/s, charge on electron =  $q = e = 1.6 * 10^{-19}$  C

mass of electron =  $m = 9.1*10^{-31}$  kg, V = ? Total energy in eV = ? Ionization energy = ?

Electric potential = 
$$V = \frac{Kq}{r} = \frac{9*10^9*1.6*10^{-19}C}{5.29*10^{-19}C} = 27.22 \text{ V}$$

Total energy = 
$$\frac{-\text{Ke}^2}{2\text{r}} = -\frac{9*10^9(1.6*10^{-19})^2}{2*5.29*10^{-11}} = -13.6eV$$

Ionization Energy =  $E_{\infty}$  -  $E_{ground}$  = 0 - (-13.6eV) = 13.6eV

12.12 The electronic flash attachment for a camera contains a capacitor for energy used to produce the flash. In one such unit, the storing the potential difference between the plates of a 750µF capacitor is 330V. Determine the energy that is used to produce the flash.

Given Data :  $C = 750 \mu 5 = 750 * 10^{-6} F$ , V = 330 V, Energy = E = ?

$$E = \frac{1}{2}CV^2 = \frac{1}{2}(750*10^{-6})(330)^2 = 40.8 J$$
 pakcity.org

12.13: A capacitor has a capacitance of  $2.5 \times 10^{-8} F$ . In the charging process, electrons are removed from one plate and placed on the other one. When the potential difference between the plates is 450V, how many electrons have been transferred?  $(e = 1.60 \times 10^{-19} C)$ .

Given Data:  $C = 2.5 * 10^{-8} F$ , V = 450V,  $e = 1.6 * 10^{-19} C$ , n = ?

$$Q = CV = (2.5 * 10^{-8})(450) = 1125 * 10^{-8} C$$

no electrons = n = 
$$\frac{Q}{e}$$
 =  $\frac{1125*10^{-8}C}{1.6*10^{-19}C}$  =  $7*10^{13}$